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#### INTRODUCTION

This report is submitted in fulfillment of the requirement of paragraph H, Part I of Contract OM-5400. It is essentially two reports within one cover: A progress report covering the period 10 September to 30 October 1959; and a summary technical report on general work undertaken in the period 14 April to 30 October 1959.

During this last half-year, this Corporation has been charged with the responsibility of determining the general principles for a high performance system to meet the following general specifications:

- 1. Very high performance;
- 2. Extensive coverage (4,000 nautical miles, 60% overlap with about 20° convergence, and 60° total transverse coverage);
- Ease of intelligence extraction (maximum scale and frame type information);
  - 4. Minimum weight (an initial target figure of 500 pounds);
  - 5. Reliability approaching 100%;
  - 6. Volume limitation dependent on specific vehicles;
  - 7. Minimum radio frequency interference; and
  - 8. Unattended operation.

The general system specifications contain many conflicting requirements. For instance, maximum scale implies a larger system and hence is not compatible with either minimum weight or small size. Similarly, extensive coverage is not compatible with minimum weight nor small size since large amounts of film must be carried to permit extensive coverage.

The high reliability requirement dictates that this inherently complex system be operationally simple: Generally this can be best accomplished by fewness of operational parts -- that is, what you don't take along can't fail; and it also implies an absence of reciprocating motions and non-uniform motions of moving parts.

Within these specifications and limitations, our primary efforts have been to obtain the high performance,—coverage, and reliability—desired. Only when a potential system met these standards has it been considered from other points of view. As a consequence, some systems are estimated to exceed the initial weight target or to be incompatible with the specific volume, which has now been selected.

As a consequence of customer scheduling requirements it has been requested that the opportunity provided by the evaluation of vehicle characteristics be used to consider general problems rather than specific details of specific systems. This has permitted rather extensive study, resulting in assurance that there are not obvious fundamental physical limitations to the successful completion of this project, and, further, has pointed the way to specific subsystem breadboarding which would be fruitful to undertake as soon as practical.

Several sub-systems required of any system (e.g. window, v/h sensor, film transport, etc.) have been extensively analysed and tested. A continuation of this thorough examination will do a great deal to increase the ultimate reliability.

In an effort to avoid bulk and unnecessary duplication in this document, previously reported progress and conclusions are not being repeated in this report. By referring to the list of pertinent documents (Appendix P), other reports containing additional data and conclusions may be located.

#### **PROGRESS**

#### GENERAL:

The progress report contained in this section covers work done during the period 10 September to 30 October. Reference should be made to previous reports (see Appendix P) for other progress statements covering the period 14 April to 9 September.

#### LIAISON:

11 September - and R.M. Scott visited the Customer to present a progress review and discuss forthcoming work and Customer requirements.

17 September - accompanied by the Customer visited the vehicle contractor for technical discussions.

13 October - The Customer and representatives of the vehicle contractor visited this contractor for technical discussions.

21 October - and R.M. Scott visited the Customer's effice for technical discussions, and also met with the Program Director for a program review and project planning discussion.

#### V/H SENSOR:

The experimental breadboard grid sensor has been extensively tested, using aerial scenes on an accurate motion (microdensitometer) stage as a simulation of moving ground. The resulting outputs have been analyzed.

Concurrently, the correlation type sensor manufactured by Avion has been proposed to us. Chicago Aerial is reported to have an automatic driftsight type sensor, but we have been unable to obtain any data.

The possibility of programming V/H has been considered. Meteorelogical

data for the operational altitudes is required before this method can be fully analyzed, and this data has been requested.

#### ARRIAL SPECTRA:

Both methods of obtaining spectra have been put into operation.

The photo-optical analyzer has been calibrated, and the scenes analyzed so far show a directional characteristic for scene frequency content.

Additional scenes should be analyzed.

The electronic analyzer generally correborates the photo-optical analyzer, but merits further utilization to properly account for some differences.

## WINDOW:

The analysis of temperature profile through the window configuration continued. The analog computer was modified to include the capability of introducing a programmed temperature profile which would simulate thermal conditions through the entire mission. The capability of evaluating the effect of cyclic cooling was also added. An analysis of computer accuracy was completed and indicated improvements were made.

More specific data, of consequence to the window design, was obtained by consultation with the vehicle manufacturer and by further engineering analysis. Temperature profiles were obtained for some specific window configurations.

The philosophy of cyclic coeling was formulated and evaluated.

Necessary cooling rates were obtained.

Quantitative data was obtained, by calculation and experiment, of the effect, on the optical wavefront, of index gradients caused by material inhomogeneties or by thermal fluctuations.

Further experimental work was done on the development of a suitable low emissivity coating. Ability to manufacture consistently the desired coating thickness, as well as the tendency of the coating to breakdown, was examined. The emissivity of a specific coating at elevated temperatures was determined by test.

The effect of thermal shock was investigated, and quantitative results were obtained. Material quality was examined in an effort to finalize a glazing type. Window size was determined for a specific system, and glazing thicknesses for this size window, for fused silica, were calculated.

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#### Q-BAY ENVIRONMENT:

Calculations were made in an effort to obtain an understanding of the effect of thermal and pressure fluctuations upon the index of refraction of air, and to establish tolerances upon these changes which would enable desired image quality to be obtained.

Experimental investigations were carried out to confirm the estitical nature of the index gradient or turbulence problem.

The seemingly necessary isothermal bay concept was discussed with the vehicle manufacturer.

#### STABILIZATION:

A preliminary analysis of rate gyro stabilization has been made.

Some preliminary thinking about inertia-torque stabilization has been done.

IMAGE MOTION COMPENSATION:

Methods of IMC have been worked out for the various comtemplated systems.

### FILM TRANSPORT:

A segmented roller (in which the individual segments have freedom of axial movement) has been designed, fabricated and tested. It is worthy of refinement, and should be compared with air-flotation "rollers".

Since several systems may require a spherical focal surface, a breadboard film transport device to move film over the curved focal surface has been designed and fabricated, and some tests have been conducted.

Substantial problems remain, and further work must be undertaken.

#### FILM EVALUATION:

The evaluation of several films was initiated. The emulsions presently being analyzed are: Eastman SO-243, Eastman SO-221, and Fuji Negative Microfilm (Fuji Photo Film Co., Ltd., Tokyo). Basic sensitometric data and resolution capabilities of these films were determined. Recent availability of a sensitometer and completion of special film testing equipment has resulted in initial efforts toward more basic and detailed analysis of pertinent emulsion characteristics.

#### CEMENTED-JOINTS:

Preliminary experimental work on cementing of mechanical joints has been undertaken. Eastman Adhesive 910 is the only bonding agent presently being tested. At the present time it appears to be thoroughly suitable, providing the surfaces to be joined have been properly prepared. Further work should be undertaken, especially in regard to bond lifetime under service conditions.

#### PROPOSAL:

The proposal and project plan for forthcoming work was submitted on 21 October in Document 68.

# SYSTEM DESIGN:

Specifications of systems under consideration and recommended for construction have been submitted in Documents 59, 62, and 69.

#### TECHNICAL CONCLUSIONS

#### Y/H SENSOR:

Each of the three possible automatic V/H systems has its own advantages and disadvantages. The automatic drift sight type of sensor must change targets quite frequently at high V/H rates. Since its field of view is narrow it can lock onto some target not of interest, such as a cloud, and yield erroneous information. Such a system could also fail to detect discontinuities such as cliffs. Its sensitivity should be good.

The correlation sensor can also have a difficult time rejecting clouds and responding rapidly to cliffs, mountain peaks, or other such discontinuities in the scene. The response time of this type of system is basically slow and its sensitivity would be good. It is a narrow field device.

The grid type sensor is a wide field device. Its output would consist of a number of frequencies if a number of different objects at different altitudes are in its field of view. The device's response time can be made rapid. The major drawback is that it depends upon the presence of one particular spatial frequency in the image of the terrain. If this frequency is not present there will be no output from the sensor. The correlation sensor depends upon a band of frequencies rather than a single frequency but this is offset by the small field of view which limits its energy acceptance. Our analysis of aerial spectra scenes indicate wide variations in spectra.

Zero crossing measuring techniques, i.e., period measurements, offer a distinct advantage both in spread of response and accuracy in the presence of noise. The experimental recordings made of the V/H sensor

output indicate the need for electronic sophistication in the actual circuitry.

Actual flight testing of the sensing heads will be necessary to evaluate accurately the magnitude of these problems. On the basis of simulated tests either method (correlation or grid) appears to be practical.

It is improbable that programmed V/H could be made accurate to better than ± 1%. However, vernier corrections from a sensor could be applied to such a programmed system to bring it within the desired-accuracy. Although a programmed V/H may not have the short term accuracy capabilities of the sensors, it may give better overall performance, and is worthy of much more consideration.

# STABILIZATION:

Rate stabilization of the platform appears practical, and its accuracy is largely dependent on the vibrational environment. Preliminary calculations indicate that if vibration isolation is not provided, the applicability of the system is limited to vibrational environments in which the maximum vibration does not exceed an angular rate of two degrees per second.

# IMAGE MOTION COMPENSATION:

Preliminary calculation indicate that good IMC correction can be obtained. The Schmidt configurations present a more attractive mechanization solution than does the Flugge system.

### WINDOW AND Q-BAY:

The construction of a window configuration to maintain the desired thermal environment appears feasible, and effects upon imagery should be more fully assessed.

The equipment bay should be isothermal to maintain image quality,

and the pressure should be no greater than about 75 mm Hg.

For the window, it is desirable to maintain minimum temperature drop through the glazing materials themselves. In order to limit radiation, a low emissivity coating should be applied to one surface bordering the gaps. It is of no consequence to which side of the gap the coating is applied. A low emissivity coating is most effective in the outermost gap, and—two coatings are more effective—than—one.—If—only—one—coating—is—used, it should be located in the outer gap.

Cooling or heat removal from the window glazings must be present, and the use of cool air for heat removal is recommended. Photographically, it is desirable to eliminate the cooling air from the gaps during an exposure. A cycle of regulated cooling air is recommended. As a maximum tolerance, the net deviation from a linear thermal gradient across the pupil cannot exceed 0.6°F per inch. Depending on allowable temperature fluctuations of the inner surface, heating may be required in the inner gap.

Further investigation is recommended to finalize material choice.

The approximate window size for the 24 inch Schmidt-System is

10.5 x 18.5 inches with slightly rounded corners and edges. Calculated

thicknesses are 0.6, 0.75, and 0.6 inches from outer to inner glazings for a

maximum of 5 psia differential across the outer glazing.

#### SERING:

As previously reported (Document 57), the turbulence introduces a random deviation of the optical ray, and the estimated standard deviation is 0.2 second in the boundary layer and 0.5 -1.0 seconds in the tropopause.

FILM TRANSPORT:

"Skidding" turns can almost surely be handled without deleterious

friction, either with a refinement of the segmented roller or with an air flotation "roller".

The deformation of film onto a curved focal surface requires additional study, but is not impossible, based on tests conducted on the breadboard transport mechanism.

#### THERMOELECTRIC COOLING:

Progress within recent years has been rapid in the application—
of semiconductor materials to thermoelectric devices. Thermoelectric
heating and cooling is quite feasible today. These devices are unique in
that they can heat or cool by reversing the direction of current flow
through the device. This means that a critical device or circuit can be
thermostated below, at, or above ambient temperature. Present methods
only allow temperature control at some elevated temperature with respect
to the ambient. The basic semiconductor material and actual devices can
readily be purchased from several sources (e.g. Philco, Admiral, Westinghouse, Texas Instruments, Ohio Semiconductor, American Standard, R.C.A.)
CEMENTED JOINTS:

The work to date has clearly established the possibility of bonding materials together with cements. It is concluded that further work should be undertaken, since the ability to utilize magnesium and beryllium, which are desirable to attenuate vibration, may depend on the practicality of bonding materials together.

#### SYSTEM DESIGNS:

Maximum effort has been expended in the general examination of nearly two dozen system design concepts. Four of these generally meet the requirements of performance, coverage and reliability, and have been described in detail in Document 69.

#### APPENDIX A

# OPTIMUM DESIGNS FOR FIXED-GRID V/H SENSORS

#### INTRODUCTION

With modern reconnaissance systems there is a very urgent need for a simple automatic, passive device which will measure the ratio

$$\frac{V}{H} = \frac{\text{Vehicle velocity with respect to ground}}{\text{Vehicle altitude above ground}}$$
 (1)

At the present time there are three basic ways of determining this ratio:

- By tracking individual objects and measuring their apparent angular velocities.
- By measuring the cross correlation between the light intensity received from two directions and computing V/H from the delay time between signals.
- 3. By measuring the frequency of signals generated by passing an optical image of the ground through a spatial filter which transmits only the desired image components.

The first method--although it is the one usually used by human beings--requires a great degree of sophistication and complexity for mechanized systems and, therefore, has not yet received much use.

The second method is simple and easily mechanized but has the disadvantage that a high capacity delay device is needed. This device usually takes the form of a tape recorder and, accordingly, has many of the problems associated with moving parts.

The third method is slightly more complex than the second, but can be built without moving parts, and can easily be designed for very high accuracy and very fast response time.

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This appendix is concerned with the third type of system, and in particular with a system in which the spatial filter assumes the form of a grid fixed in the image plane of an optical ground viewing system.

Expressions are derived which show how the system response depends on various system parameters, and from these expressions one can choose the optimum parameters.

# BASIC PRINCIPLE OF OPERATION

plane of the lens, and a photocell behind the grid. Let this system move with velocity V at a fixed altitude H above a point source of light located on the ground. As the system moves past the light, the image of the point will move across the grid. The effect of the grid is to periodically attenuate the light so that the electrical signal from the photocell is a periodically pulsed current. If the grid spacing is 2a and the lens focal length, F, then the frequency of the pulsed photocell current is

$$\frac{\nabla}{H} \frac{F}{2a} = \text{frequency.}$$
 (2)

Where f = focal length of optical system which projects an image of the ground on the grid

2a = grid spacing (lines/unit length).

The only restrictions on the operation of this type of system is that the imaging system resolution be somewhat better than  $\frac{1}{2a}$  lines/mm and that there is sufficient signal strength from the ground to give a workable signal to noise ratio in the photocell. Since even for high performance systems, a typical value for  $\frac{1}{2a}$  would be 5 lines/mm for an f/3, 12-inch focal length system, there is no problem with resolution.

# ESTIMATE OF AVAILABLE SIGNAL

Since at the present time very little is known about the characteristics of various types of ground terrain, as a crude estimate, we will assume that the ground appears to be uniform except for a dense random array of areas of diameter b and contrast c. Table I shows estimates of b and c for various types of terrain.

TABLE I	<u>p</u>	- <u>c</u>	<u>bc</u>
Choppy water	2 feet	.05	.1 feet
Sagebrush	2 feet	.2	.4 feet
Wooded area	20 feet	.5	10 feet
Residential housing	50 feet	.5	25 feet
City	100 feet	.5	50 feet

If one compares the total light flux received from two randomly selected areas, each of area A, the average absolute fractional flux difference will be

$$\left\langle \frac{|\Delta B|}{B} \right\rangle^{2} \frac{bc}{A}$$

The area,  $A^2$ , is related to the sensor field of view by the relation

$$A^2 = \frac{a^2nK}{f^2}$$

where

n I the number of grid lines

ak = the length of the lines

H I camera altitude.

If the photocell has a sensitivity, N, and the sensor optics an aperture, D, the sinusoidal output of the photocell will be

$$i_{AC} = \frac{N^4 \quad D^2 \quad a^2 \quad nk}{\mathcal{D}^2 \quad f^2} \quad \frac{\overline{B} \quad bc \quad f}{a \quad \sqrt{nk} \quad H \quad /8} = N \quad \frac{4 \quad D^2 \quad a \quad \sqrt{nk} \quad bc \quad \overline{B}}{\sqrt{8} \quad H \quad f \quad \mathcal{D}}$$

where  $\overline{B}$  is the average ground brightness.

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To see how this looks, consider a 12-inch focal length f/3 system with 1/2 a = 5 lines/mm,  $\overline{B}$  = 10 foot candles n = k = 500 lines, N = 1 amp/lumen, bc = . 4 ft. (sagebrush desert), H = 100,000 ft.

Under these conditions we find that

$$\frac{i_{AC}}{N}$$
 = 2.05 x 10<sup>-7</sup> 1umen

or

$$i_{AC} = 0.205 \mu \text{amp}$$
.

which is a quite useable current. If V/H = 0.01 radians/sec the average frequency of this sinusoidal signal would be 30 cycles/sec., while f or V/H = 0.1 rad/sec., this frequency would be 300 cps. By using photomultiplier photodetectors, this current could be increased by a hundred fold to give potential operation over desert in near darkness.

Since V/H is proportional to this frequency, all that remains to be done is to measure this frequency. We proposed to do this by counting the number of times the A.C. component of the signal crosses zero. For a sine wave input of frequency  $\frac{V}{H} \cdot \frac{F}{2a}$  there are  $\frac{V}{H} \cdot \frac{F}{a}$  zero crossings per second.

# COMPARISON WITH AUTOCORRELATION SYSTEM

The useable signal in an autocorrelation typeV/H system has been computed under the same assumptions as the fixed grid system. Here the useable current is

$$1_{\text{rms}} = \frac{\text{N } 4\text{D}^2 \text{a bc B}}{\pi \text{H } \text{f} \sqrt{8}}$$

which differs by a factor  $\sqrt[7]{nk}$  from the grid system current. Here, however, the assumptions about the ground characteristics do not apply as much as in

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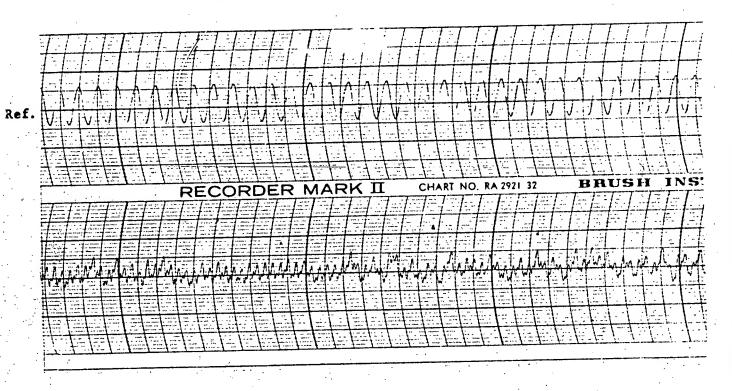
the case of the grid system, so that the two systems will probably have about the same net useable signal strengths.

#### EXPERIMENTAL RESULTS

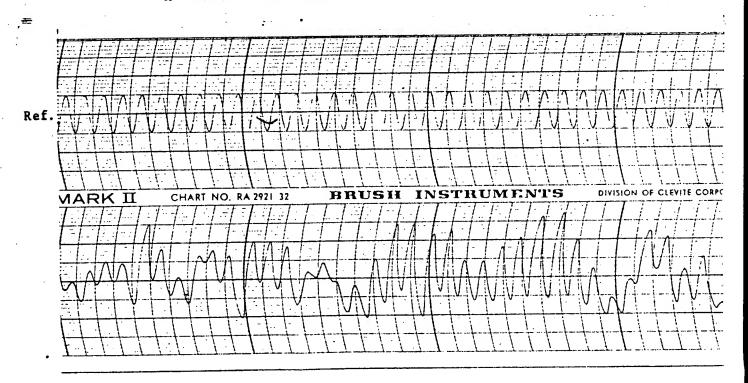
Recordings of the output of A/fixed grid V/H sensor are given in Figures A-1 to A-6. The characteristic control of the control

Approved For Release 2004/05/13: CIA-RDP89B00739R000900070001-6 GRID = 6 lines/mm

Reference channel = 24 cps at 0.2 volts/line = 125 mm/secRecorder speed



No Filter Negative = HR-73B Camera X - Axis = .05 volts/line



Low-Pass Filter

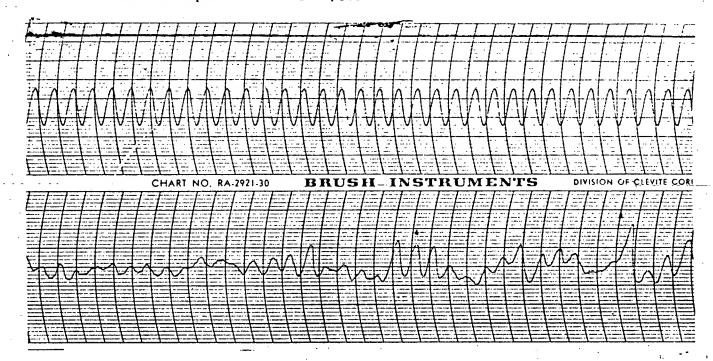
Figure A-1

Approved, Egg Release 2014/95/13 et AA-RDP89B00739R000900070001-6 X - Axis = .05 volts/line (increased sensitivity due to recharged

hattary (11 cht gource)).

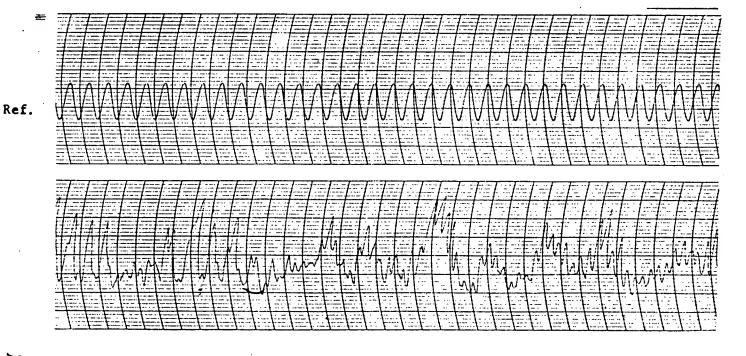
# Approved For Release 2004/05/13 : CIA-RDP89B00739R000900070001-6 GRID = 6 lines/mm

Reference channel = 24 cps at 0.2 volts/line Recorder speed = 125 mm/sec



Negative = HR-73B Camera X - Axis = 0.2 volts/line

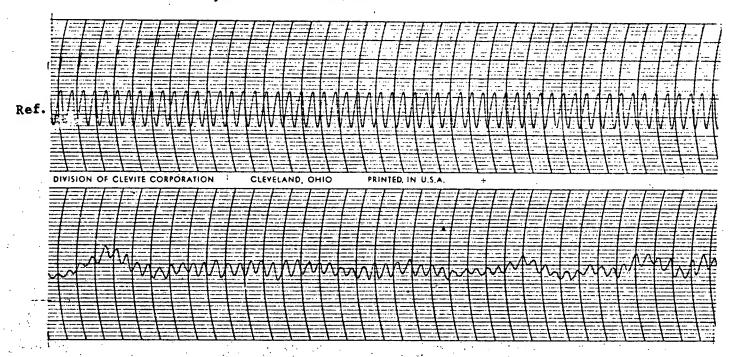
Ref.



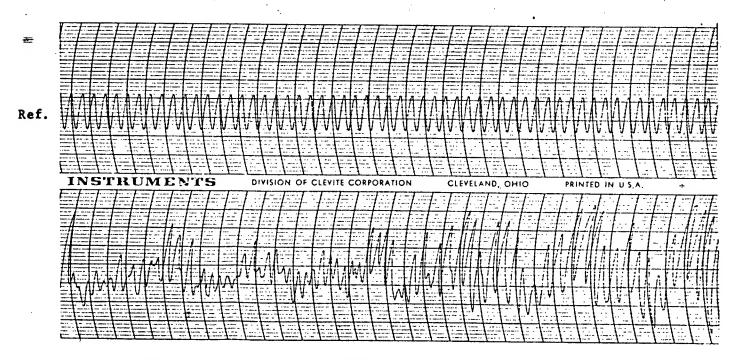
Negative = 501 Tracking Camera X - Axis = 0.2 volts/line

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Reference channel = 40 cps at 0.2 volts/line Recorder speed = 125 mm/sec.



Negative = HR-73B Camera X - Axis = 0.2 volts/line

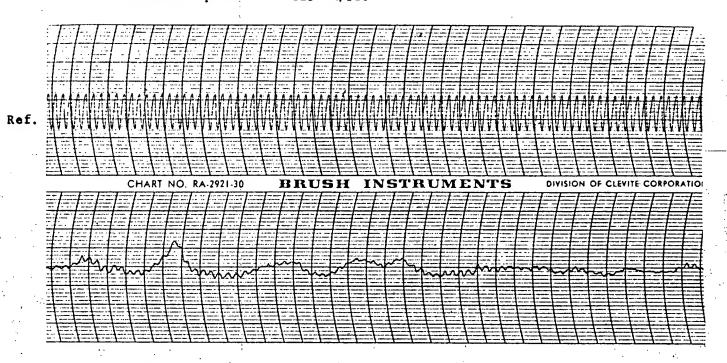


Negative = 501 Tracking Camera X - Axis = 0.2 volts/line

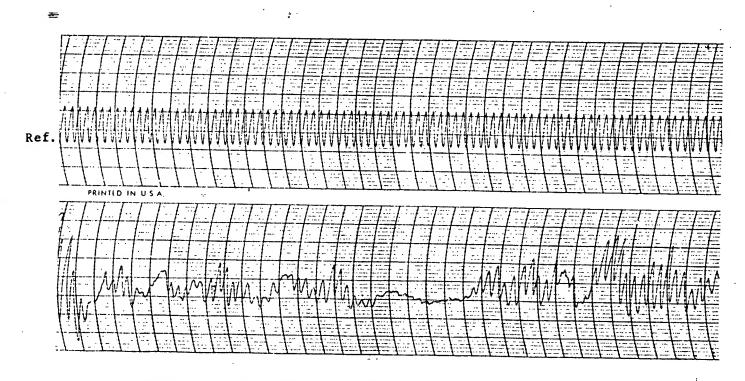
Figure A-3

GRID = 15 lines/mm

Reference channel = 60cps at 0.2 volts/line Recorder speed 125 mm/sec



Negative = HR - 73B Camera X - Axis = 0.2 volts/line



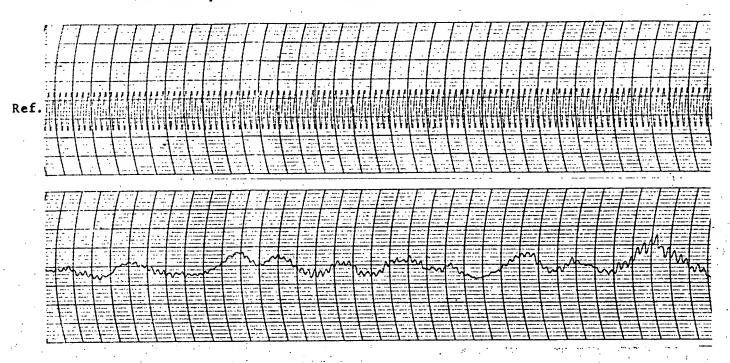
Negative = 501 Tracking Camera
X - Axis = 0.2 volts/line
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Figure A-4
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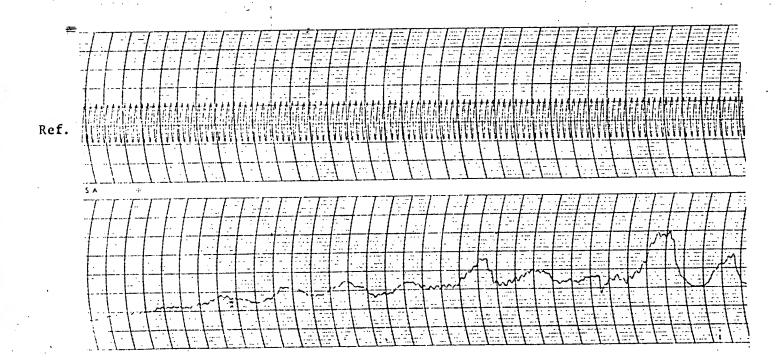
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# Approved For Release 2004/05/13: CIA-RDP89B00739R000900070001-6 GRID = 20 lines/mm

Reference channel = 80 cps at 0.2 volts/lime Recorder Speed = 125 mm/sec



Negative = HR - 73B Camera X - Axis = 0.2 volts/line



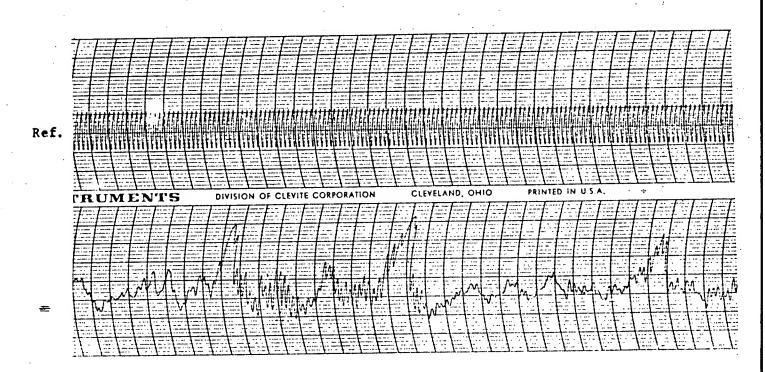
Negative = 501 Tracking Camera X - Axis = 0.2 volts/line

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• GRID = 25 lines/mm

Reference channel = 100 cps at 0.2 volts/line

Recorder speed = 125 mm/sec



Negative = 501 Tracking Camera

X - Axis = 0.2 volts/line

Figure A-6

#### APPENDIX B

## FREQUENCY SPECTRUM OF A FINITE GRATING

The spectrum of an infinite grating is given by the well known

Fourier series expression for a square wave. If the grating is not infinite

the spectrum is obtained by convolving the spectrum of the window function,

or length of the grating, with that of the line spectrum of the grating itself.

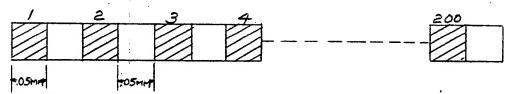
The effect of this is to widen the lines into a sin \*x\* function whose width

depends upon the length of the window function; the wider the window, the narrower

the function becomes. When the window function becomes infinitely long then

the sin x/x function becomes a single frequency or line.

Consider the grating below consisting of 200 transmitting and 200 non-transmitting spaces, each one of which is 1/20 mm wide



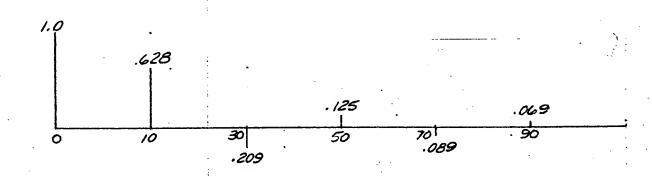
The basic line spectrum is given by the following:

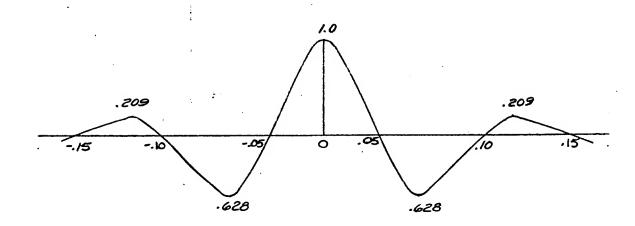
Spatial frequency cycles per mm	Amplitude Coefficient Normalized
. 0	.1
10	2
30	-2/3
50	2/5
70	2/7
90	2/9

as illustrated in Figure B-1. The window function is equal to a spatial pulse 20 mm long. The spectrum of this is a sin x/x function with minima at  $\frac{1}{20}$  cycles per mm,  $\frac{1}{10}$  c/mm,  $\frac{1}{20}$  c/mm,  $\frac{1}{20}$  c/mm,  $\frac{1}{20}$  c/mm,  $\frac{1}{20}$  c/mm, etc. Its maxima are at 0 cycles per mm,  $\frac{1}{20}$  c/mm,  $\frac{1}{20}$  c/mm, etc., as illustrated in Figure B-1.

If each line in the basic spectrum is replaced by the above function by substituting the line frequency for the zero frequency (using the superposition theorem) we now have the spectrum of the grating.

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SPECTRUM OF A GRATING
FIG. B-1

It is of interest to note that the basic pass frequency of the grating, 10 cycles per mm, is widened to a band roughly equal to 10 ½ .05 cycles per mm. Thus an error can exist in the presence of an irregular terrain frequency distribution. To minimize this potential error the number of lines in the grating should be as large as possible. Roughly the possible error is given by the product of 100 times the reciprocal of the number lines in the grating.

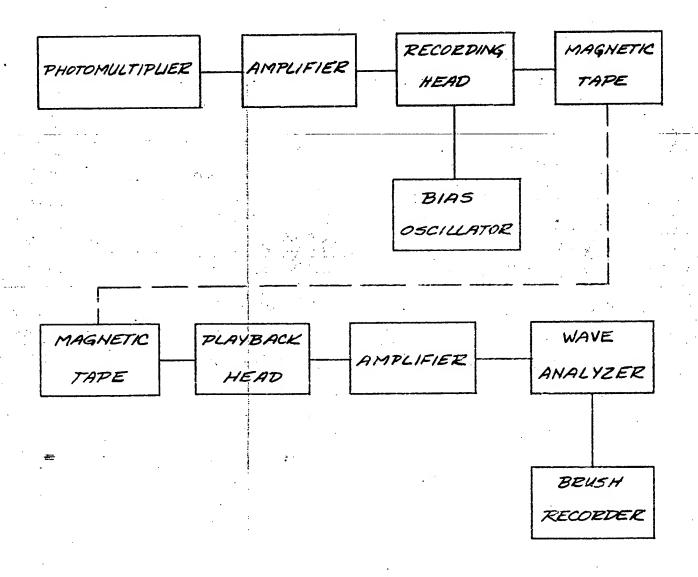
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#### APPENDIX C

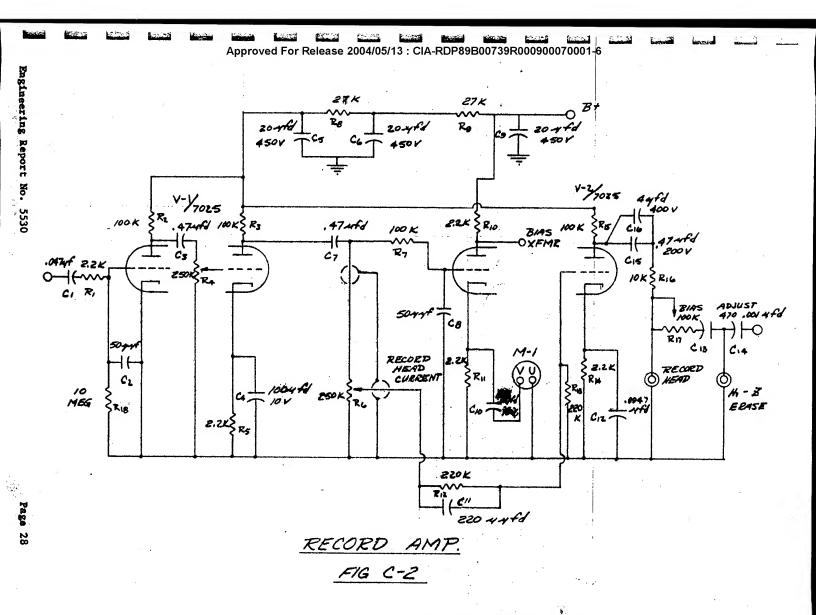
#### ELECTRONIC SCENE ANALYSIS

The essential elements of the electronic scene analyzer are shown in the block diagram, Figure C-1. A Leeds & Northrup microdensitometer has been modified to obtain a higher scanning speed than is normally obtained with this instrument. Normally the fastest scan speed is 5/6 mm per second. The temporal frequencies obtained from scanning a negative are given by the product of the scan speed times the spatial frequencies in the negative. For a range of spatial frequencies from 1 cycle per mm to 200 cycles per mm, the temporal range would be 5/6 cycles per second to 167 cycles per second. This is a difficult range for the direct recording process. This is possible to record with the FM process but the stability requirements on the transport mechanism become very stringent, and the mechanism becomes expensive. For example, a / 0.2% variation in tape speed at a center frequency of 3000 cycles means a / 12 cps variation in playback and recording which means an error of / 10 cycles per mm in the measurement of the spectrum. Increasing the scanning speed to 14.6 mm per second increases the temporal frequency range to 14.6 -2920 cycles per second. It is practical to record to 20 cycles per second and lower. The difficulty in the low frequency range is in reproduction. Hence, by recording at 3 3/4 inches per second and playing back at 7 1/2 inches per second, the temporal range becomes 29.2 to 5840 cycles per second. This is a very feasible range to work with.

A photomultiplier head was made for the L&N to replace the phototube pick-up supplied with this instrument. The signal from this photomultiplier is then amplified in the recording amplifier, Figure C-2, and recorded on standard 1/4 inch wide magnetic tape on a Viking series 85 Transport. A

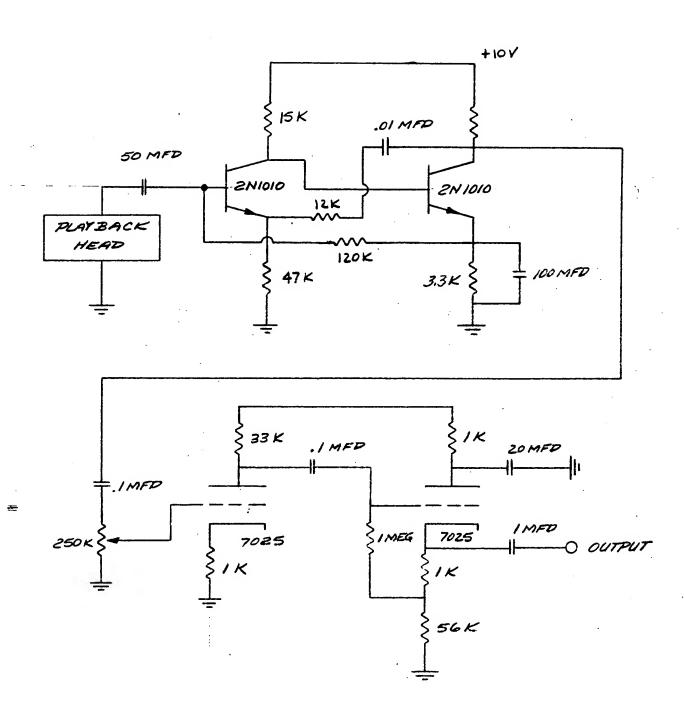


ELECTRONIC SCENE ANALYZER ; FIG. C-1



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second playback head is used to simultaneously monitor the recording. The tape, which is used in the form of a 55-inch continuous loop, is then played back through the playback amplifier, Figure C-3. This signal is then put into the General Radio Wave Analyzer. The frequency selector dial of the wave analyzer is driven by a constant speed motor and the output of the analyzer is recorded on a Brush Mark II Recorder. The General Radio Wave Analyzer is not ideal for this work because the calibration of its frequency selector dial is not a linear function of angle of rotation. Thus, the frequency scale of the recordings is not linear and the recordings are cumbersome to interpret. This difficulty will be resolved by the use of the Hewlett Packard Wave Analyzer, which is being procured for this program. The frequency calibration of this instrument is a linear function of shaft rotation, so the frequency scale on the final recording is linear.



PLAYBACK AMPLIFIER SCHEMATIC FIG. C-3

#### APPENDIX D

# STABILIZATION BY RATE GYRO PEEDBACK

The purpose of this analysis is to determine, within first order accuracy, the feasibility of utilizing a rate feedback closed loop control system for stabilizing a platform with respect to its inertial axis. The performance characteristics of a commercially available subminiature precision rate gyro and a low inertia servo motor have been utilized in making this analysis (see references below).

The following assumptions have been made:

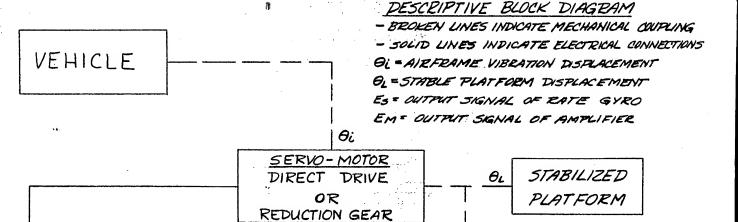
- 1. The vibrational environment and mechanical vibration isolation described in Reference 1 is assumed.
  - 2. Non-linearities in all components are assumed negligible.
- 3. An ideal gear reduction unit is assumed (gear inertia, friction and backlash are negligible) or a direct drive motor is used.
  - 4. Time delay of the servo motor's winding is negligible.
- 5. Time delay of the rate gyro's torque windings (if one is used in place of spring loading) is negligible.
  - 6. Time delay of the amplifier is negligible.
- The Exploratory Analysis of Isolation Philosophies for the Protection of an Ultra-Sensitive "R" System (Project 2570).
- John Oster Manufacturing Company Catalog -- Low Inertia Servo-Motor, Type 15-5153.
- 3. The U.S. Time Corporation, Gyro Division Catalog -- "Subminiature Rate Gyro" Model No. 40.

- 7. The only source of noise within the closed loop system is assumed to be that of the rate gyro as specified by the manufacturer, i.e., amplifier and servo motor noise (due to hysteresis and harmonics) are assumed negligible.
- 8. The effect of linear acceleration of the airframe on gyro performance is negligible.
- 9. The effects of temperature variations on component performance is negligible.
- 10. The angular rate of deviation of the stabilized platform from its inertial axis must not exceed 1/10 of 1° per second.
- 11. The moment of inertia of the fully equipped platform is estimated not to exceed 4000 lbs.-in-sec. 2.

The approach used in analyzing the performance of the proposed rate feedback stabilisation system was to assume a theoretical rate feedback system in the form of a system block diagram where each component in the system is represented by a block with its input and output signal sonnections to other blocks indicated by arrows which indicate the direction of the transmitted signal (see Figure D-1).

The component dynamic is now examined. In order to reduce the complexity of the problem, simplifying assumptions have been made regarding the dynamic characteristics of each of the components (see Assumptions). We believe these assumptions to be justified since a first order approximation of the performance of the proposed system is acceptable at this stage in the development and the results will indicate the optimum performance that can be expected from physically realizable equipment.

AMPLIFIER



RATE

GYRO

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RATE FEEDBACK STABILIZATION SYSTEM
FIG. D-1

pifferential equations which determine the dynamic performance of each of the idealized components are now derived and, by means of the Fourier transformation, transformed into an operational transfer function of frequency which will provide the gain (or attenuation) and phase shift which the component causes on a sinusoidal input signal of a given frequency. The transfer function is now associated with its corresponding blocks in the system block diagram and, by means of conventional feedback control theory, operational transfer functions for both open and closed loop response of the system are derived. The parameters of these transfer functions are related to the inertia, drag, spring constant and other physical parameters of the components.

The next step in the analysis is to select a servo motor capable of supplying the peak power and torque requirements of the stabilized platform. By neglecting bearing friction and viscous drag, the platform may be assumed to present a purely inertial load to the motor. Using the estimated maximum moment of inertia, the maximum allowable angular velocity of the stabilized platform, and the expected vibration environment, the peak torque, peak power and average power requirements of the load were determined. Using these calculated values, a suitable servo motor was selected (see Reference 2) and the required gear ratio determined. Referring to torque-speed curve and torque-versus control voltage (at stall) curve, the motor parameters were determined and supplied to the open and closed loop transfer functions.

The following procedure was used to estimate the performance characteristics and dynamic parameters that a suitable rate gyro would require.

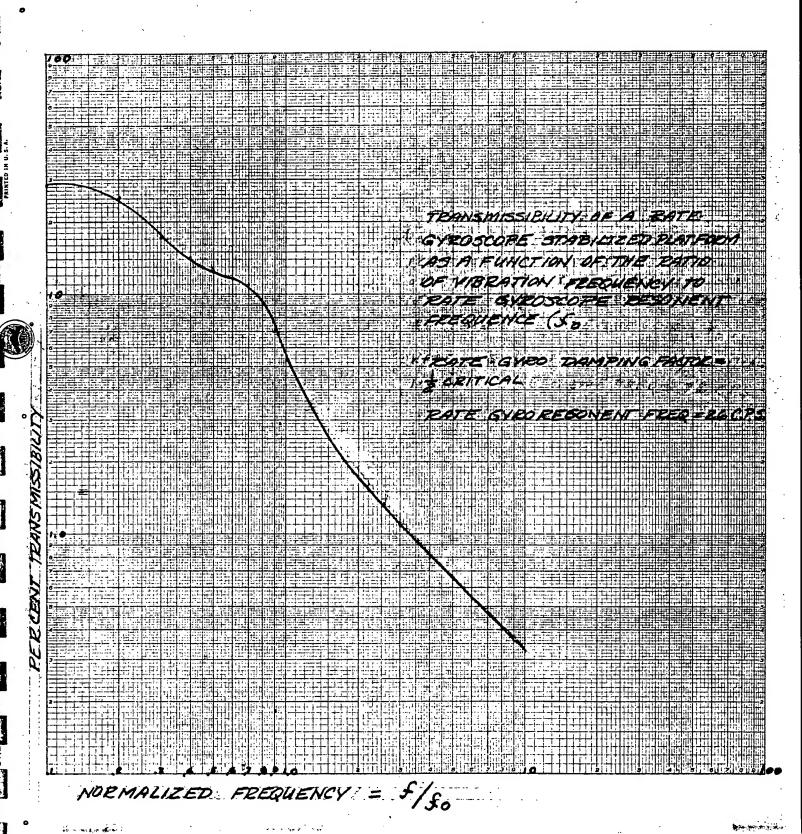
A good compromise between speed of response and overshoot for many practical feedback control systems is obtained when the system parameters are adjusted so that the gain margin of the open loop transfer function is (-10 db) and its

phase margin is (30 deg.). Solving the open loop transfer function for the above gain margin yields an expression which shows that the required open loop gain constant is directly proportional to the product of the rate gyro's damping factor and resonant frequency.

The solution of the open loop transfer function for a phase margin of 30 deg. indicates that the rate gyro damping factor should be three tenths. Substituting the derived relations and values into the closed loop transfer function gives us an expression for this function in which the only unknown parameter is the resonant frequency of the rate gyro. The absolute magnitude, i.e., gain of the closed loop transfer function, defines the "transmissibility" of the proposed rate feedback stabilization system, shown in Figure D-2.

The selection of the rate gyro was made on the basis of required full scale range, resolution, zero errors and residual noise. All of these factors were found to fall well below the maximum tolerable values required by the stability performance requirements for the rate gyro which was selected (see Reference 3). The nominal damping factor of this rate gyro is 1/2 of critical damping and, thereby exceeds the optimum damping factor (3/10 of critical). Therefore, response of this rate gyro is somewhat more sluggish than that which is desired and may require a higher open loop gain and, consequently, more amplification than that which is required by the optimum rate gyro.

Resonant frequency of the selected gyro is 26 cps. This frequency is permissible if the transmissibility characteristics of the vibration isolators approximate system "A" (described on page 26 of Reference 1), but is somewhat closer to the resonant frequency of system "B" (same reference).



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However, if the anticipated vibrational environment approximates that provided in Reference 1 (page 11 of 26), the coincidence of the vibration isolation and stabilization systems resonance should not result in excessive vibrations at 26 cps. The maximum transmissibility at 26 cps for the rate stabilization system "B" vibration isolators is three percent, giving a system transmissibility at resonance of 0.15% while the transmissibility when system "A" isolators are used would be less than 0.04%. Class B system would allow a maximum vibrational environment of 67 deg/sec. at 26 cps which is far in excess of what is to be expected from the vehicle at this frequency.

The effect of residual gyro noise on the noise level of the closed loop stabilization system output was next evaluated. All other possible sources of noise were considered negligible in this analysis. The expected maximum noise level of the closed loop stabilization system due to the presence of rate gyro noise should not be greater than twelve percent of the gyro's redisual noise. This residual noise is given by the manufacturer as not exceeding 0.08 deg/sec maximum. The system noise should, therefore, not exceed 0.09 deg/sec. a tolerable value.

The results of the analysis, described above, leads to the following conclusions concerning the practicality of a rate feedback stabilization.

- 1. Rate stabilization of the stabilized platform is practical if a precision rate gyroscope of the type described in Reference 3 is used to generate the angular rate signal and the vibrational environment and isolation approximates that described in Reference 3.
- 2. If vibration isolation is not provided, the applicability of the system is limited to vibrational environments in which the maximum vibration does not exceed an angular rate of two degrees per second.

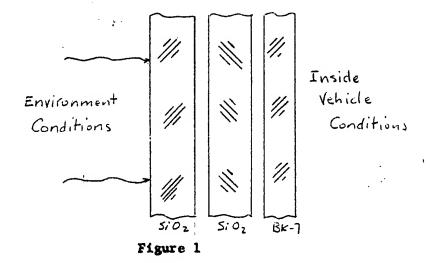
- 3. Damping factor for the selected rate gyro is somewhat higher than the calculated optimum value indicating some sluggishness in the gyro's response to input angular rate deviations. However, rate gyros with lower damping factors than that of the selected unit are commercially available if required.
- 4. Gyro noise effect should not prove to be a problem in the rate feedback stabilization system.

#### APPENDIX E

THERMAL EVALUATION OF WINDOW PROBLEM

The solution of transient heat flow equations is necessary for the proper analysis of the thermal aspect by the window problem. An initial solution was attempted by mathematical methods, but was found to be too complex for convenient theoretical analysis. An electrical analog method was derived for the solution of these equations. Not only did the analog method afford a means of obtaining the basic heat data, but it also enabled a convenient and efficient means for evaluation of various proposed window design parameters and configurations.

The initial analog design was based upon a simulation of the existing experimental window configuration; two eight inch diameter, 0.878 inch thick fused silica glazings and one eight inch diameter, 0.480 inch BK-7 inner glazing, Figure 1. This was done to enable a comparison of analog data with that of actual experiment.



The design of the analog computer is based on the following:
The properties of Corning 7940 fused silica are:

\* Specific heat = 
$$Cp = 0.2008$$
  $\frac{cal}{gm^{\circ}C} = 0.2008$   $\frac{Btu}{lb^{\circ}F}$ 

\* Density = 
$$c = 2.2 \text{ gm/cc} = 0.0793 \frac{1b}{in^3}$$

\* Thermal Conductivity = 
$$K = 0.0037$$
  $\frac{\text{cal cm}}{\text{cm}^2 \text{ sec}^{\circ}\text{C}} = 0.075$   $\frac{\text{Btu in}}{\text{in}^2 \text{ hr}^{\circ}\text{F}}$ 

\* (Taken from data compiled by Corning Glass Works)

Average values in the range between -20°F to 550°F were used since the quantities do not change appreciably with temperature.

$$Cp(=(0.2008) \frac{Btu}{1b^{0}F} (0.0793) \frac{1b}{in^{3}} = 0.0159 \frac{Btu}{in^{3} o_{F}}$$

$$\frac{\text{Cp?}}{\text{K}} = \frac{0.0159 \frac{\text{Btu}}{\text{in}^3 \text{ op}}}{0.075 \frac{\text{Btu in}}{\text{in}^2 \text{ hr}^{\text{op}}}} = 0.213 \frac{\text{hr}}{\text{in}^2} = 767 \frac{\text{sec}}{\text{in}^2}$$

#### CONDUCTION:

For convenience, each fused silica glass glazing is divided into = :
seven equal sections of width, d.

$$\therefore d = \frac{0.878}{7} = 0.1252 \text{ in.}$$

Electrically, the thermal properties of these sections are represented by tee sections as in Figure 2.

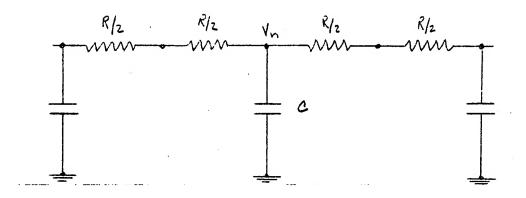


Figure 2 - Tee Sections

Where the resistors are analogous to the resistance of the material to conduct heat across its section, the capacitor is an analogy of the ability of the material to retain heat, and the voltage drop across the tee is analogous to the temperature drop across the section.

$$V_{n}^{(t)} = \frac{1}{c} \int_{0}^{t} \frac{(V_{n+1} - V_{n})}{R} + \frac{(V_{n-1} - V_{n})}{R} dt + V_{n}^{(0)}$$

$$= \frac{1}{Rc} \int_{0}^{t} (V_{n-1} - 2V_{n} + V_{n+1}) dt + V_{n}^{(0)}$$
Eq. (1)

From transient heat conduction relations,

$$\frac{d^{2}\Theta(x,t)}{dx^{c}} = \frac{C_{P}C}{k} \frac{d\Theta(x,t)}{dt_{w}}$$
Eq. (2)

Where  $\oplus$  = temperature, and is a function of  $\alpha$  and t.

d= thickness of the section

} ≈ time

x= distance to window section

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Since,

$$\frac{d^2\theta_n}{dx^2} \cong \frac{\theta_{n+1} - z\theta_n + \theta_{n-1}}{d^2}$$

Eq. (3)

where 
$$\Theta_{n} = \Theta(nd + \frac{d}{2}, t)$$

Then from equations (2) and (3),

$$\frac{d^2\Theta_n}{dx^2} \cong \frac{\Theta_{n+1} - 2\Theta_n + \Theta_{n-1}}{d^2} = \frac{C_F C}{K} \frac{d\Theta_n}{dt_{n-1}}$$

or, 
$$\theta_{n+1} - z\theta_n + \theta_{n-1} = \frac{z^2 C_p \ell}{k} \frac{d\theta_n}{d\ell}$$
 Eq. (4)

Differentiating Equation (1),

$$RC \frac{dV_n}{dt_c} = (V_{n+1} - 2V_n + V_{n-1})$$
Eq. (5)

Note that equations (4) and (5) are of the same form.

A time scale factor, S , is now introduced that relates computer time,  $t_{\rm c}$  , with the actual window time,  $t_{\rm w}$  .

$$\dot{t}_{\omega} = S \dot{t}_{c}$$
 Eq. (6)

Introducing Eq. (6) to Eq. (5)

$$SRC \frac{dV_n}{dt_w} = (V_{n+1} - 2V_n + V_{n-1})$$

Ba. (7

Since voltage is the analog of temperature, then from eqns. (4) and (7)

$$SRC = \frac{d^{2}C_{p}C}{K} = (.1252)^{2} in^{2} (767) \frac{se}{in^{2}}$$

$$= 12.05 sec$$

$$C = 1 \mu f$$

Then RC = 0.039 sec.

And 
$$S = \frac{12.05}{.039} = 309$$

Time Scale Factor =  $\leq$  = 309

At equilibrium, the flow of heat through each section is

$$h = -K \frac{d\Theta}{dx}$$
but  $\frac{d\Theta_n}{dx} \cong \frac{\Theta_n + \frac{1}{2} - \Theta_n - \frac{1}{2}}{d}$ 

$$\therefore h = -\frac{K}{d} \left(\Theta_n + \frac{1}{2} - \Theta_n - \frac{1}{2}\right)$$

Electrically, this is analogous to the current through n

or 
$$i_n = -\frac{\sqrt{n+1/2-1/n-1/2}}{p}$$
 Eq. (9)

and  $\frac{K}{d}$  is analogous to  $\frac{1}{R}$ 

Now, let the relationship between voltage and temperature be

$$T = aV + b$$
 Eq. (10)

where a and b are constants

Introducing the relationship of eqn. (10) to eqn. (8),

$$\mathbf{h} = -\frac{\mathbf{K}}{\mathbf{d}} \left[ \left( \mathbf{a} \vee_{\eta + \gamma_{\mathcal{L}}} + \mathbf{b} \right) - \left( \mathbf{a} \vee_{\eta - \gamma_{\mathcal{L}}} + \mathbf{b} \right) \right]$$

$$\mathbf{h} = -\frac{\mathbf{a}\mathbf{K}}{\mathbf{d}} \left( \sqrt{\gamma_{\eta + \gamma_{\mathcal{L}}}} - \sqrt{\gamma_{\eta - \gamma_{\mathcal{L}}}} \right)$$

And from eqn. (9)

$$h = + \frac{aK}{d} R 1_n$$

Eq. (11)

$$\frac{KR}{cl} = \frac{0.075 \text{ in hu of }}{1.252 \text{ in .}} \times \frac{1 \text{ hu}}{3600 \text{ sec}} \times 39,000 \text{ ohms}$$

$$= 12.0 \frac{\text{Btu}}{\text{In}^2 \text{ sec }^2 \text{k}} \times \frac{\text{folts}}{\text{amp}}$$

$$\therefore h = + 12.0 \text{ a in } \frac{\text{Btu}}{\text{m}^2 \text{ sec }^2 \text{k}} \times \frac{\text{folts}}{\text{onp}} \times \frac{\text{ok}}{\text{folts}} \times \text{amp} = \frac{\text{Btu}}{\text{in}^2 \text{ sec}}$$
Eq. (12)

#### RADIATION:

The radiation of heat across the gap between the windows is represented thermally by

$$h_{rw} = 0 \frac{\xi_1 \xi_2}{\xi_1 + \xi_2 - \xi_1 \xi_2} \left[ \Theta_{n+1/2} + -\Theta_{m-1/2} + \right]$$
 Eq. (13)

where dis the Stefan-Boltzmann constant = 0.1713 x  $10^{-8} \frac{\beta t \omega}{f t^2 h r^{\circ} R^{+}}$  $\epsilon_{\star}$  = emissivity at surface of first window

emissivity at surface of second window

 $\Theta_{7i} + V_i =$  temperature at surface of first window

 $\Theta_m - h_z =$  temperature at surface of second window

If the ratio of  $\theta_1 + \frac{1}{2}$  to  $\theta_m - \frac{1}{2}$  (in absolute measurement) is up to 2, then

And from eq. (13)

$$h_{vad} = \sigma \frac{\epsilon_{i} \epsilon_{c}}{\epsilon_{i} + \epsilon_{c} - \epsilon_{i} \epsilon_{c}} 4(\theta_{auc}^{3})(\Theta_{n} + \gamma_{c} - \Theta_{m} - \gamma_{c})$$
Eq. (14)

Eq. (14) is of the same form of eq. (9), thus

$$\dot{L} = \frac{h_{\text{tad}}}{4 \, \text{a} \, \sigma \, \epsilon, \epsilon_{\text{c}}} \frac{h_{\text{tad}}}{\epsilon_{\text{l}} + \epsilon_{\text{c}} - \epsilon, \epsilon_{\text{c}}} \frac{3}{2} \, \text{P}$$

Since, from eq. (12)

$$h = 12.0 \text{ a } i_n$$

then

and

$$\mathbf{R} = \frac{12.0}{46} \frac{6.67}{6.62} \theta_{av}^{3}$$

Eq. (15)

Substituting into eq. 15 for various  $\Theta_{\rm exc}$ , the following values of R are found:

Case 1 - No coatings on window surfaces

				6,62	7- 4/662 - ×10-6
	<u>\theta ° k</u>	€,	Ez	6,+62-6,62	P = 466.62 $6.+62.6.62$ $6.+62.6.62$
•	300	. 89	. 89	. 800	3. 96
	×.400	. 87	. 87	.770	1.82
	500	. 84	. 84	.724	99
<del>~</del>	600	.81	.81	. 681	.61
	700	.77	.77	. 626	.418
	•				

# Case 2 - One window surface coated, the other not coated

300	. 89	. 2	. 195	17.00
400	. 87	.2	. 194	7.22
500	. 84	. 2	. 193	3.71
600	.81	.2	.191	2.18
700	.77	.2	. 189	1.38

## Case 3 - Both window surfaces coated

<i>6</i> %	<u> </u>	Ez	€, €z €,+€z -€,	$\frac{12.0}{\epsilon_z}$ $\frac{12.0}{\epsilon_1 + \epsilon_2 - \epsilon_1 \epsilon_2}$	David X10 - Lagolar
300	.2	. 2	.111	30.00	
400	.2	.2	.111	12.60	·
500	.2	.2	.111	6.46	**
600	<b>.2</b>	. 2	.111	3.74	, ) · · · · · · · ·
700	.2	.2	.111	2.38	

Since the emissivities are functions of temperature, an average slope

(taken at the mid-point of the range) must be found that will fit the relationship
between resistance and temperature.

Thus for Case 1:

For Case 2:

$$\left(\frac{G_z}{G_1}\right)^{\frac{1}{2}} = \frac{R_z}{R_1^2}$$

$$\left(\frac{700}{300}\right)^{\frac{1}{2}} = \frac{1.38}{17.00}$$

$$2.33^{\frac{1}{2}} = \frac{.0813}{.2.97}$$

$$\frac{1}{2} = \frac{.0813}{.2.97}$$

And for Case 3:

$$\frac{\left(\frac{\Theta_{z}}{\Theta_{1}}\right)^{k}}{\left(\frac{\Theta_{z}}{\Theta_{1}}\right)^{k}} = \frac{R_{z}}{R_{1}}$$

$$\frac{2.33}{30.00} = \frac{2.38}{30.00} = .0794$$

$$k = -3.00$$

A curve was drawn based on measured values of detector resistance vs. voltage.

Transposing values to correspond with the slopes calculated above,

corresponding voltages are calculated below.

The slope relationship is:

$$\frac{L \log R}{d \log T} = \frac{nT}{T-b}$$

Eq. (16)

## For Case 1:

From "Detector Resistance vs. Voltage" curve, n = -3.41

$$\frac{d \log C}{d \log T} = -2.68 \qquad \frac{\pi T}{1-b} = \frac{-3.41 (500)}{500-b}$$

$$\frac{-2.68}{500-b} = \frac{-3.41 (500)}{500-b}$$
and  $b = -13b$  (65000k)

Since T = aV + b

then 500 = 65a - 136

and a = 9.8

Thus, the corresponding voltages for each 8 value taken are:

<u>9</u>	<u>v</u>
<b>3</b> 00	·· 44.5
400	54.7
500	65.0
600	75.1

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<u>e</u>	<u>v</u>
700	85.4
0	13.7

#### For Case 2:

$$\frac{d \log R}{d \log T} = -2.97 \frac{\pi T}{T-b} = \frac{-3.55(500)}{(500-b)}$$

$$\therefore -2.97 = \frac{-3.55(500)}{500-b}$$

$$\therefore -2.97 = \frac{-3.55(500)}{500-6}$$

and b = -97.8

since T = aV + b

then 500 = 45a - 97.8

<u>e</u>		<u>v</u>
300		30.0
400		37.5
500		45.0
600	÷ ·	52.6

#### For Case 3:

$$n = -3.62$$

$$\frac{d \log K}{d \log T} = -3.00 \frac{717}{7-b} = \frac{-3.62(500)}{500-b}$$

700

$$\frac{1}{100} = \frac{-3.62(500)}{500-6}$$

and b = -103.3

then 500 = 38a - 103.3

and a = 15.9

60.0

<u>•</u>	. <u>V</u>
300	25.4
400	31.6
500	38.0
600	44.2
700	50.5

#### CONVECTION:

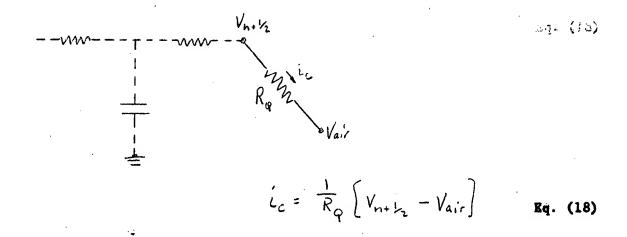
The thermal convection of heat caused by an air stream through the gap between the windows is represented as in Figure 3 below

$$\theta_{air} \qquad h_{conv.} = Q \left[ \theta_{n+1/2} - \theta_{air} \right]$$
where  $Q = Convection Constant$ 

$$\theta_{n+1/2}$$

Figure (3) Convection Schematic

Electrically, the heat convection is simulated by Figure 4 below.



Since T = aV + b, and from eqs. (17) and (18)

$$i = \frac{h}{\varphi a R_{\varphi}} = \frac{12.0 a i}{\varphi a R_{\varphi}} = \frac{12.0 i}{\varphi R_{\varphi}}$$
 amps

and  $R_Q = \frac{12.0}{Q}$  ohms where Q is in units of  $\frac{Bhc}{Sec. in^{2.0}K}$  Eq. (18a) It is intended that the value of  $R_Q$  will be chosen to suit various window parameters.

The last window is of BK-7 rather than fused-silica quartz and is 0.480 in. thick. Because of the differences, it becomes necessary to calculate the total resistance value required in the analog of the last window.

For BK-7

$$Cp = 0.199 \frac{Btu}{1b^{o}F}$$

$$e = 160 \frac{1b}{ft^3} = 0.093 \frac{1b}{in^3}$$

$$K = 5.5 \frac{Btu in}{ft^2 hr^0 F} = 0.0382 \frac{Btu}{in hr^0 F}$$

$$\frac{\text{Cp } \ell}{K} = 0.482 \, \frac{\text{hr}}{\text{in}^2} = 1735 \, \frac{\text{sec}}{\text{in}^2}$$

From eqs. (4) and (7):

> has been established as being 309

$$C = 1 \mu f = 1 \times 10^{-6} farad$$

$$d = .480 = 0.096$$
 in. (using five sections)

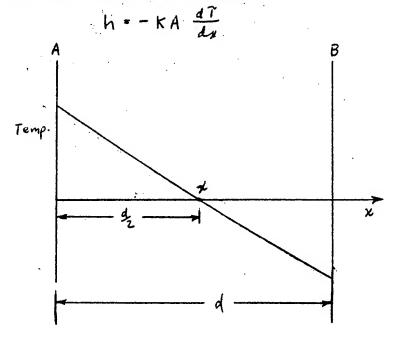
$$R = (.0092) in^2 (1735) in^2 = .051 x 10^6 ohms$$
  
309 (1 x 10<sup>-6</sup>) farad

#### ANALYSIS OF ANALOG ACCURACY:

The errors inherent in the electrical analogy of the thermal heat transfer across the window system are briefly discussed below.

The mathematical outline of the computer involves differential equations which may be functions of complex form. The differential quantities were approximated by making them equal to finite increment quantities or, in other words, dx was approximated by Ax (eq. (3), eq. (8). Seven sections were used in the analogy of the quartz thickness.

Using a fused silica glass window divided into seven equal sections of width, d, the heat flow through each section is



We can approximate over a small interval the temperature function by a taylor expansion about point x.

At edge B the temperature can be written as

$$\mathcal{T}_{(x+\frac{d}{2})} = \mathcal{T}_{(x)} + \mathcal{T}_{(x)} \frac{dz}{dz} + \frac{\mathcal{T}_{(x)}''}{2} \frac{d^2}{4} + \frac{\mathcal{T}_{(x)}'''}{8\cdot6} + \dots$$
 (Eq. 20)

At edge A the temperature can be written as

$$\gamma_{(x+\frac{1}{2})} = \gamma_{(x)} - \gamma_{(x)}' \frac{d_2}{d_2} + \frac{\gamma_{(x)}'' \frac{d^2}{d_2}}{2 \cdot 4} - \frac{\gamma_{(x)}''' \frac{d^3}{d_2}}{8 \cdot 6} + \dots$$
(Eq. 21)

$$T_{A} - T_{B} = T_{(4)} d + \frac{T'''(1) d^{3}}{6 \cdot 4} + \dots$$
(Eq. 22)

were T'(x) is the True Temperature gradient at x.

Rewriting eq. (22) we have

$$\frac{T_A-T_B}{d}=T'_{(1)}+\frac{T''_{(1)}}{G}\cdot\frac{d^2}{4}+\ldots$$

However, after the first 5 minutes T(x) in the first plate is sufficiently linear such that

$$\frac{T_A - T_O}{d} - T_{(x)}$$

$$\leq c 1$$

From this result we estimate that the major effect of this approximation is to give an error in the time scale of 3 minutes or less.

Inedetermining the temperature dependent parameters, namely, thermal conductivity, specific heat, and emissivity, the mean value of each parameter was calculated over the temperature range of operation. These approximations are considered to introduce no greater error than the magnitude of error inherent

in the compilation of the original data for fused silica.

The heat transfer coefficient for forced convection in the second gap is dependent on physical properties of the coolant and the configuration of the apparatus. The physical properties were calculated at the mean of the cooling air. The plate was assumed to be a square configuration. The error due to these assumptions is considered to be almost negligible.

Further sources of error are due to innate inaccuracies in the electrical components (for example, capacitor leakage and tolerance in resistor values). The expected errors due to component inaccuracies were calculated to be about 5.4%.

The errors induced by components can be found as follows:

We denote the N elements of a sample by  $x_1$ ,  $x_2$ ,  $x_3$ +...  $+x_N$ , where the values of each element are distributed independently of the other values and according to the given distribution function x. The variable x has a mean  $\xi$  and variance  $\xi$ .

The sum and the mean of the values

$$S_{x} = x_{1} + x_{2} + \dots + x_{N}$$

$$\overline{x} = \frac{1}{N} (x_{1} + x_{2} + \dots + x_{N})$$

vary from sample to sample.

Now

$$M(S_x) = M(x_1) + M(x_2) + \dots + M(x_N) = N \xi$$

$$V(x) = V(x_1) + V(x_2) + \dots + V(x_N) = N \xi^{-1}$$

where M is mean and V is variance.

Consequently

$$H(\overline{x}) = \frac{\sigma}{2}$$

$$V(\overline{x}) = \frac{\sigma^2}{N}$$

The standard error is defined as the square root of the variance thus

The standard error of 25 resistors and 21 capacitors is

#### Capacitors

$$x_1 = x_2 = x_3 = x_N = 20\%$$

$$\delta = \left[\frac{\xi fi (x_1 - \overline{x})^2}{\xi fi}\right]^2 = 20\%$$

$$N = 21 \qquad \sqrt{N} = 4.6$$

$$S.E. = \frac{20\%}{4.6} = 4.4\%$$

#### Resistors

$$x_1 = x_2 = x_3 = x_N = 5$$
  
 $0 = 5$   
 $0 = 5$   
 $0 = 5$   
 $0 = 5$   
 $0 = 5$   
 $0 = 5$ 

Total error in system  $\simeq 4.4\% + 1.0\% = 5.4\%$ 

The error caused by approximating the  $(\theta_1^4 - \theta_2^4)$  term in the radiation relation by  $4(\theta_1 - \theta_2)(\theta_{ave}^3)$  eq. (14) can be calculated.

For the radiation equation:

$$\theta_1^4 - \theta_2^4 = 4 (\theta_1 - \theta_2) \theta_{ave}^3$$
 Eq. (23)

The range of values for  $\theta_1/\theta_2$  which make the above approximation good to within (x%) can be found as follows:

Percent accuracy = 
$$\chi = \frac{4 \theta_{ave}^{3} (\theta_{1} - \theta_{2})}{\theta_{1}^{4} - \theta_{2}^{4}}$$
 Eq. (24)

but

$$\theta_{am} = \frac{\theta_1 + \theta_2}{2}$$

Thus eq. (24) become

$$\chi = \frac{50 (\theta_1 + \theta_2)^3 (\theta_1 - \theta_2)}{\theta_1^4 - \theta_2^4}$$

$$= \frac{50 (\theta_1 + \theta_2)^2 (\theta_1^2 - \theta_2^2)}{(\theta_1^2 - \theta_2^2) (\theta_1^2 + \theta_2^2)} = \frac{50 (\theta_1^2 + \theta_2^2)}{\theta_1^2 + \theta_2^2}$$

$$\chi = 50 \frac{\left(\frac{\theta_{i}}{\theta_{2}} + 1\right)^{2}}{\left(\frac{\theta_{i}}{\theta_{2}}\right)^{2} + 1}$$
Eq. (25)

Rewritting eq. (25)

$$(x-50)(9/92)^2-100(9/92)+(x-50)=0$$
 Eq. (26)

Using equation 26 the following values of  $\theta_1/\theta_2$  were calculated for various values of

% Error (X)	θ <sub>1</sub> /θ <sub>2</sub>
0	1.00
1	1.22
2	1.33
5	1.59

Z Error (≠)		e <sub>1</sub> /e <sub>2</sub>
8		1.84
10	•	2.00
13.9	·× .	2.25
15.6	•	2.50
17.6		2.75
20.0		3.00

The maximum value of  $\theta_1/\theta_2$  about 2.5, occurs between surface 2 and 3 of the proposed window configuration. The simulation inaccuracies are presumed to be about 5%. The use-of empirical relations for heat convection are probably accurate within  $\pm 30\%$ .

The analog is designed to be a one dimensional model and does not take into account conduction, convection, or radiation to the side walls or the window supports, although some corrections can be easily made if these effects are small.

The recording instrument can be read accurately to the nearest quarter of a scale division ( $\pm$  1/8). This can amount to an error of 2.2F<sup>O</sup> or a total error of 0.4% over the temperature range.

# DETERMINATION OF COOLING AIR TEMPERATURE AND RATE:

The primary objective of the cooling air is to maintain the inner surface of the window at a preselected temperature; 130°F has been used in this analysis. However, the manner in which this is accomplished will ultimately be a determining factor in establishing the thermal profile of the window.

Cooling air will necessarily be introduced from one edge of the inner gap. This will result in a thermal gradient, in the direction of air flow, in both adjacent glazings. The allowable gradient in each glazing is determined by such factors as tolerance to index of refraction changes in the glazing and in the equipment bay environment, and effect of non-uniform thermal expansion of the glazings. These tolerances have been discussed in Appendix 7.

Various investigators have analyzed the heat transfer characteristics for laminar flow between parallel plates. Their data indicates that the coefficient of heat transfer increases linearly with cooling air velocity in a particular parameter range. Beyond that range, it varies nonlinearly; the degree of nonlinearity being determined by the window and cooling air parameters.

The inner glazings will develop a thermal gradient which has a close correspondence to the temperature of the cooling air across the window. To minimize the thermal gradient in the inner glazing, it is necessary to introduce a high rate of cooling at a small temperature difference relative to the inner glazing. The limiting case is one which soaks the inner glazing in 130°F air to maintain it uniformly at 130°F,

The gradient in the middle glazing is somewhat different in behavior, since it has a thermal history different than the inner glazing. The magnitude of the gradient can be reduced by tipping one or both of the glazings to form a wedge-shaped gap. Such a configuration will increase velocity

with a decreasing AT, between glasing and air. However, since cooling may vary nonlinearly with velocity, such a wedge shaped gap may result in a non-linear gradient. The magnitude of tolerable non-linearity becomes a major consideration, as set by optical considerations (Appendix F).

Therefore, in any case, some gradient will result. Based on these considerations, a cooling rate and cooling air temperature can be established which avoids or minimizes harmful optical degradations caused by thermally induced index changes. Further work is necessary in understanding the optical behavior of the glazings and equipment bay environment, and also in establishing more detailed thermal data before this value can be determined.

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The thermal analog is a one dimension model. The analysis of thermal profile obtained by using the analog computer is representative, for any one set of input conditions, of a section through the window, such as the leading edge. The required coefficient of heat transfer to obtain desired cooling of the inner surface along the section analyzed was determined. This coefficient is a function of temperature difference of the air to inner surface temperature and velocity. Thus, although temperature of the cooling air and its subsequent velocity have not yet been finalized, a complete temperature profile through the one dimensional model can be obtained.

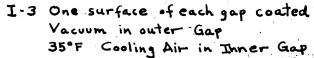
Figures E-4 and E-5 show the temperature profile for the six window surfaces, for such a section. The input heat profile into surface 1 is obtained from mission profile data and corresponding temperature.

j

WINDOW CONFIGURATION

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Surface No

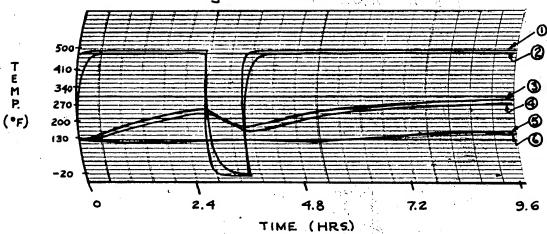
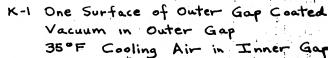


FIG. E-4

# TEMPERATURE

Approved For Release 2004/05/13: CIA-RDP89B00739R000900070001-6

WINDOW CONFIGURATION



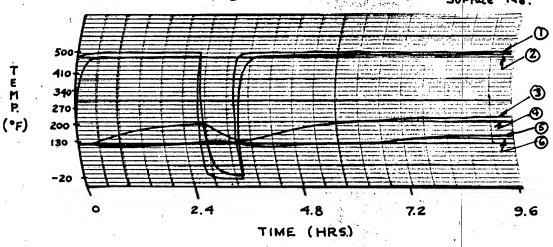


FIG. E-5

#### APPENDIX F

# INVESTIGATION OF IMAGE DISTORTION IN WINDOW AND EQUIPMENT BAY

Discarding all influences upon the image forming wavefront prior to the window (which have been discussed in Document 57) the wavefront from an infinite object may be considered plane. The quality of the image which is produced by such wavefronts is determined by such factors as diffraction effects, correction of the image forming optics, and distortion of the incoming plane waves. The required correction and permissible diffraction limits have been established which will result in such image quality as to result in the desired resolution. It is necessary to establish tolerances upon allowable wave deformation resulting from bay environment and window effects in order to maintain the necessary image quality.

The criterion upon which this analysis is based is that deviations of 1/10 wave per inch from a place wavefront are tolerable. This is equivalent to a ray deviation of 1 second of arc or  $4.8 \times 10^{-6}$  radians.

One source of wavefront distortion is index fluctuations or inhomogeneties of the window material. Fluctuations of index as well as index gradients have been determined for suitable window materials. These values are listed in Figure F-1.

It is not a straightforward analysis to ascertain the allowable index fluctuations based on the established deformation tolerances. This is because the nature of the fluctuations themselves have a decided influence upon their relative effect. For example, several sharp index "spikes" which exceed what would normally be excessive limits are actually more tolerable than continuous fluctuations which have wavey shapes whose amplitudes are within

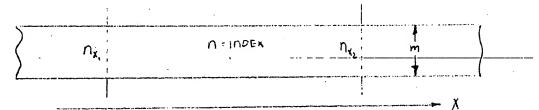
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#### COMPARISON OF OPTICAL PROPERTIES Material 1723 7900 7940 Fused Silica Vycox Aluminosilicate **Property** Refractive Index 1.546 (1) 1.458 (1) 1.459 (1) (Nd line) Homogeneity $3.8 \times 10^{-5}$ 3 x 10<sup>-6</sup> $8 \times 10^{-6}$ (1) (1) Index gradient/inch/inch thickness Homogeneity (for 20 inch diameter blank) $2 \times 10^{-5}$ (1) $1 \times 10^{-5}$ (1) Index gradient/center to edge/inch thickness Change of Index $100 \times 10^{-7}$ (3) Change of Temperature (OC) at .6µ Transmission, percent 1/4" thickness 90 - 92 (1) 91 - 92 (1) 92 (1) (1) Total Emissivity 300°F .90 (1) . 87 (1) . 82 . 81 600°F .90 .88 900°F .79 . 89 . 87 (3) N.B.S. Vol. 53, p. 188 (2) Measured value (1) Data from Corning Glass

Figure F-1

and shape of index fluctuations in each of the materials to most efficiently minimize the distortions from this cause.

An initial approach to the problem, which considers the allowable index variation across the pupil is as indicated in the following diagram.



Optical Path Length = mm

Optical Path Difference 
$$(x_2 - x_1) = a(n_{x_2} - n_{x_1})$$

$$OPD = m \Delta n$$

$$\frac{1}{10} \lambda = 6 \times 10^{-6} \text{ cm for } \lambda = .6\mu$$

Therefore

$$\bigwedge_{m} n = \frac{6 \times 10^{-6}}{m}$$

where  $\Delta$  n is the tolerable index change per inch.

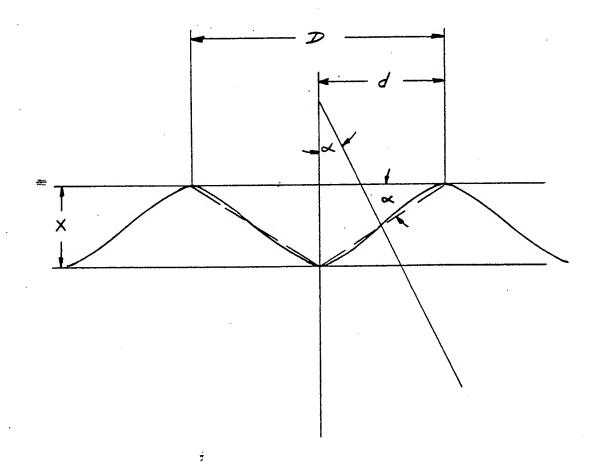
Evaluating An for several thicknesses, we obtain

thickness (cm)	Δn
1	6 x 10 <sup>-6</sup>
2	3 x 10 <sup>-6</sup>
3	2 × 10 <sup>-6</sup>
. 4	1.5 x 10 <sup>-6</sup>
5	1.2 x 10 <sup>-6</sup>

According to this analysis, in a 5 cm thick window, a linear gradient which exceeds  $1.2 \times 10^{-6}$  change in index across the pupil is intolerable. The effect of a

linear gradient is only to translate the image laterally with respect to the film plane, with no resulting image deterioration. The allowable image translation is dictated by pointing accuracy requirements and upon tolerable resultant chromatic effects. For a monochromatic system,  $\triangle$  n  $\le$  10<sup>-1</sup> could be tolerated. Therefore translations resultant from  $\triangle$  n = 1.2 x 10<sup>-6</sup> are certainly tolerable.

A more realistic analysis is to consider the index fluctuations to have-the-form of sine-waves. This type of gradient is much less tolerable than the linear one, since it has the effect of spreading the energy of the image. Consider a 1 second energy spread (± 1/2 sec.). The sinusoidal gradient can be represented as a varying linear function as shown in the figure below:



0% = tolerable ray deviation

= ± .5 second

 $= \pm 2.4 \times 10^{-6}$  radians

$$\frac{x}{d} = x$$

$$x = \infty d$$

for d = 1.2 cm

$$x = \frac{2.4 \times 10^{-6}}{1.2}$$

$$x = 2 \times 10^{-6}$$
 cm

 $x = OPD = m \Delta n$  where m = thickness

$$\triangle n = \frac{2 \times 10^{-6}}{m}$$

and since  $2d = D \approx 1$  inch

∆ n represents index gradient per inch across pupil.

Evaluating An for various thicknesses, we obtain:

thickness (cm)	n
1	2 x 10 <sup>-6</sup>
2	1 x 10 <sup>-6</sup>
3	.66 x 10 <sup>-6</sup>
4	.5 x 10 <sup>-6</sup>
5 :	.4 x 10 <sup>-6</sup>

The validity of this analysis depends largely on whether a linear approximation of the sine-wave is a realistic representation of energy distribution.

The fact remains that it is possible to make acceptable schlieren windows of comparable thickness from such material as fused silica. Corning estimates an index gradient of 8 x 10<sup>-6</sup> per inch across the aperture, for a one

inch thick blank (see Figure F-1). This is an order of magnitude in excess of the tolerance calculated above, eventhough schlieren windows require similar wave deformation tolerances as are applied here.

Some improvement in minimizing the effects of index fluctuations can be brought about by local figuring of the polished window. This has the effect of locally varying the window thickness to compensate for varying index, maintaining:

#### mn = constant

This is more feasible for a schlieren window than for this configuration, since the schlieren window is one piece of glass, used at normal incidence. Parallax which is present in a spaced three glazing configuration would diminish the effectiveness of this technique.

The analysis of index variations within the glazing material indicates that further investigation is necessary to establish whether available material is of sufficiently good homogeniety as to not impair optical performance. In particular, it is desirable to understand more about the shape and statistical nature of these fluctuations.

The effect of a thermal gradient in the glazing materials on a plane optical wavefront must be determined to establish the tolerable magnitude and shape of such a gradient. For the purpose of analysis the gradient can be divided into two components, one normal to the window surface, and one parallel to the window surface.

The effect of a thermal gradient normal to the parallel surfaces of a glazing material on a plane wavefront would be a uniform retardation across the entire wavefront. The wavefront itself would be undistorted after having passed through the window, and consequently the image quality would be unaffected.

A method for computing the effects of a lateral thermal gradient on an incident wavefront has been investigated theoretically by G.G. Sliusarev<sup>1</sup>. The investigation is based on the change in shape of an optical component under the influence of non-uniform heating as well as the effect of the gradient on the index of refraction. The results indicate that for an optical element in the shape of a plane parallel plate, the deviation of a light ray is directly proportional to the thermal gradient g, and to the nominal thickness e, of the optical element. For a plate of refractive index n, linear coefficient of thermal expansiong, the coefficient of change of refractive index with temperature  $\beta$ , the deviation  $\hat{\xi}$ , is given by:

$$\mathcal{E} = \operatorname{eg} (n-1) + \operatorname{eg} \beta = \operatorname{eg} \left[ (n-1)\alpha + \beta \right] = \operatorname{Keg}$$
 Eq. (1)

A plane parallel plate under the influence of a temperature gradient would expand by different amounts along its length, becoming wedge shaped and displaying the optical properties of a prism. A ray of light incident on the plate would therefore be deviated by an amount  $\mathcal{E}_i$  given by:  $\mathcal{E}_i = \operatorname{eg} \propto (n-1)$ . In addition, there would be a second deviation due to the change of refractive index with temperature given by:

$$\xi_2 = eg\beta$$

The total deviation is the sum of these two deviations and is given by the Sliusarev equation, (1).

For the particular case of a fused silica plate:

$$\alpha = 3 \times 10^{-7} \text{ per}^{-9} \text{F}$$

$$\beta = 55.5 \times 10^{-7} \text{ per}^{-9} \text{F}$$

$$n = 1.459$$

$$K = \left[ (1.459 - 1)(3 \times 10^{-7}) + 55.556 \times 10^{-7} \right] = 5.6933 \times 10^{-6}$$

$$E = (5.6933 \times 10^{-6}) \text{ eg}$$

OPTICS AND SPECTROSCOPY, Vol. VI, No. 2, February 1959 - "Influence of Temperature Gradient of Glass of Optical Systems on the Image Produced by the Latter"

The total deviation of a ray is therefore a linear function of the local value of the thermal gradient. A plot of the deviation against the gradient is shown for various thicknesses in Figure F-2. The shape of the thermal gradient will cause different effects upon an impinging plane wavefront. The simplest case of a linear gradient will result in a wave deviation, but no wave distortion. This will have no effect on the image except a displacement of the image laterally along the focal surface. Such an image displacement, in the magnitudes anticipated, is tolerable. The next simplest case is that of a gradient assuming a quadratic form. The effect of such a gradient would be to introduce cylindrical power, and distort the plane wavefront along one axis. The result would be astigmatism of the image. The tolerance for the amount which a thermal gradient can depart from linear can be determined by establishing a value for the allowable wave deformation.

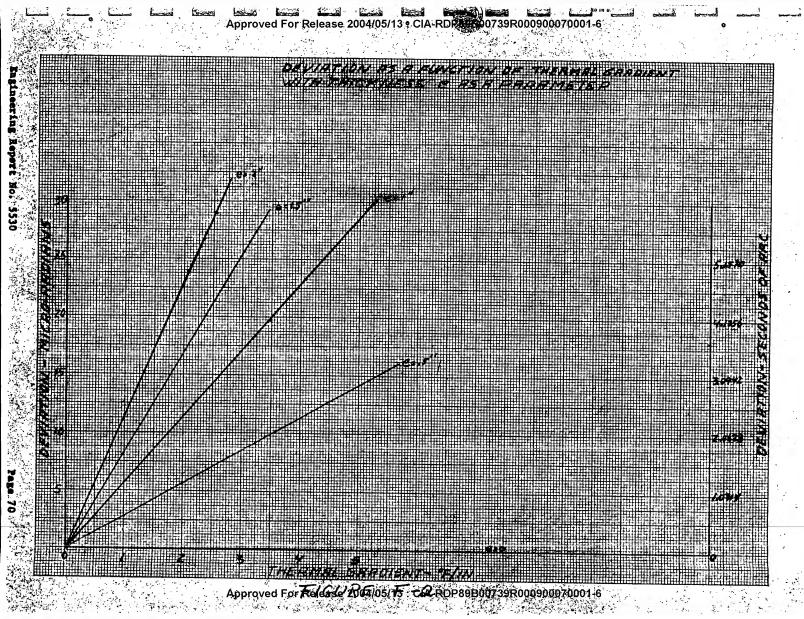
In general the same approach holds for any variation in the thermal gradient as long as this variation is not too rapid.

The specific configuration under consideration is that of three glazings, separated by gaps. A cooling air flow in the inner gap will cause a thermal gradient along the two inner glazings. For the condition of vacuum in the outer gap, any thermal gradient across the outer glazing caused by the gradient of the inner glazings would be of second order consideration. Inasmuch as the gradient produced in the two inner glazings is in the same direction, they can be considered as one thick glazing, 1.5 inches for this analysis.

医对子口病 化抗结合物的过程 计重要的 医阿里克勒氏线 有整理的复数 医骨折 计工作 医乳色性 医骨孔生活的 医毛毛科

If  $\mathcal{E}_1$  = Keg1 is the deviation at some arbitrary point along the length of the plate and  $\mathcal{E}_2$  = Keg2 the deviation at a second point, the  $\Delta \mathcal{E}$  = Ke(g2-g1) = Ke $\Delta$ g or  $\Delta$ g =  $\frac{1}{\text{Ke}}\Delta\mathcal{E}$ . For a plane wavefront striking the plate at normal incidence, the maximum allowable change in g, the thermal gradient, across the entire pupil, is:

$$\Delta g = \frac{1}{(5.6922 \times 10^{-6})(\frac{3}{2})}$$
 5 x 10<sup>-6</sup>



based on  $\Delta \xi \leq 5 \times 10^{-6}$  radians.

This value, unfortunately, even though imposing a tight limit, considers only the case of normal incidence. For oblique incidence, the allowable gradient variance decreases appreciably. This case has not yet been analysed.

Finally the nature of index fluctuations in the air present in the optical path must be analyzed.

The dependence of optical index on gas density is given quite accurately

by

$$(n-1) = \frac{\rho}{\rho_0} \quad (n_0-1)$$

where n = index of refraction, and

 $\rho$  = density.

It is also known that

$$\frac{\rho}{\rho o} = \left(\frac{P}{760}\right)\left(\frac{273}{T}\right)$$

for a constant volume, where

P = Pressure in mm. of Hg

T = Temperature in K.

Consequently, we can express the dependence of index on pressure and temperature by

$$(n-1) = \left(\frac{P}{760}\right)\left(\frac{273}{T}\right) (n_0-1).$$

<sup>-</sup> Jenkins & White, "Fundamentals of Optics" 2nd Ed., Page 251

<sup>-</sup> American Institute of Physics Handbook, page 3-56

For 
$$\lambda = .6\mu$$
,  $n_0 - 1 = 2.92 \times 10^{-4}$ , when  $P = 760 \text{ mm.}$ ,  $T = 273^{\circ} \text{K}$ . So,  $(n-1) = 1.05 \times 10^{-4} \frac{P}{T}$ ,

and therefore

$$\frac{\partial n}{\partial P} = \frac{1.05 \times 10^{-4}}{T} \quad \text{per um. Hg}$$

$$\frac{\partial n}{\partial T} = -1.05 \times 10^{-4} \quad \frac{P}{T^2} \quad \text{per } ^{O}K.$$

Thus we arrive at the following table:

Condition	P = 1/3 atm = 250 mm		P = 1/10 atm = 75 mm.		
ariant	$T = 110^{\circ} F = 316^{\circ} K$	$T = 130^{\circ} F = 328^{\circ} K$	$T = 110^{\circ} F = 316^{\circ} K$	$T = 130^{\circ} P = 328^{\circ} I$	
∂n ∂P (per ma Hg)	3.3 x 10 <sup>-7</sup>	3.2 x 10 <sup>-7</sup>	3.3 x 10 <sup>-7</sup>	3.2 x 10 <sup>-7</sup>	
- <u>9 n</u> 9 <b>T</b>	2.6 x 10 <sup>-7</sup>	2.4 x 10 <sup>-7</sup>	7.8 x 10 <sup>-8</sup>	7.3 x 10 <sup>-8</sup>	

#### Furthermore

.

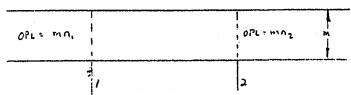
$$\Delta n = \frac{\partial n}{\partial P} \Delta P + \frac{\partial n}{\partial T} \Delta T$$

$$= \begin{pmatrix} \frac{\partial n}{\partial P} & \frac{\partial P}{\partial T} & + \frac{\partial n}{\partial T} \end{pmatrix} \Delta T$$

$$= \begin{pmatrix} \frac{\partial n}{\partial P} & + \frac{\partial n}{\partial T} & \frac{\partial T}{\partial P} \end{pmatrix} \Delta P ,$$

and the last two expressions allow calculation of  $\Delta n$  as a function of either  $\Delta T$  or  $\Delta P$  alone, providing the functional relation of P and T is known.

Now, consider two light beams passing through a gas layer m meters



thick. The optical path difference is (mn1 - mn2) or m &n. This difference

must everywhere be less than about  $1/10\lambda$  where  $\lambda$  = wavelength of light.

If we assume m = 0.5 meter,

$$\frac{\lambda}{10\text{m}} = \frac{.6 \times 10^{-6}}{10 \times .5} = 1.2 \times 10^{-7}$$

Consequently  $\triangle h \le 1.2 \times 10^{-7}$  is required, and this is nearly achieved when

$$\triangle$$
 P = .38 mm Hg (T = constant)  
 $\triangle$  T = .5 °K (P = 1/3 atmosphere)  
 $\triangle$  T = 1.5 °K (P = 1/10 atmosphere)

It can also be achieved in wider limits of either  $\triangle P$  or  $\triangle T$  provided  $\frac{\triangle P}{\partial T} > 0$ 

since  $\frac{\partial n}{\partial P} > 0$  and  $\frac{\partial n}{\partial T} < 0$ . That is, if increasing pressure is accompanied

by increasing temperature (or both decreasing), then  $\triangle n$  is reduced. For a Boyle's Law gas, at least,  $\frac{\partial P}{\partial T} > 0$  always.

However, the nature of turbulence is not well understood. There is some question as to whether it follows the laws of an ideal gas, as indicated above.

Consider the case of adiabatic conditions where:

$$T^{\chi} P^{1-\chi} = constant$$

Evaluating the constant at operating conditions of 130°F and 1/10 atmosphere

$$T^{\ell} P^{1-\ell} = (328)^{\ell} (75)^{1-\ell}$$

$$= \frac{3300}{5.9}$$

$$= 560$$

Therefore  $T = 560 \text{ P}^{\frac{6-1}{7}}$ 

$$\frac{\partial \mathbf{T}}{\partial \mathbf{P}} = \frac{8-1}{8} = 560 \frac{1}{8} = \mathbf{P} \frac{8-1}{8} = \frac{1}{8}$$

$$= \frac{\sqrt{-1}}{6} \cdot 560^{\frac{1}{6}} - p^{-\frac{1}{6}}$$

$$= \frac{.41}{1.41} \cdot (560)^{.71} \cdot p^{-.71}$$

$$= 25.9 \cdot p^{-.71}$$

at P = 75 mm Hg

$$\frac{\partial T}{\partial P} = 1.20$$

From the previous analysis, we have

$$\frac{4n}{\Delta P} = \left(\frac{3n}{3P} + \frac{3n}{3T} \frac{3T}{3P}\right)$$

substituting

$$\frac{\Delta n}{\Delta P} = 3.2 \times 10^{-7} - (7.3 \times 10^{-8} \times 1.24)$$
 $\frac{\Delta n}{\Delta P} = 2.3 \times 10^{-7}$ 

for 
$$P = 75$$
 mm

$$T = 130^{\circ}F$$

and 
$$\frac{\Delta n}{\Delta T} = \left(\frac{\partial n}{\partial P} \frac{\partial P}{\partial T} + \frac{\partial n}{\partial T}\right)$$

substituting:

$$\frac{\Delta n}{\Delta T} = (3.2 \times 10^{-7}) (.8) -7.3 \times 10^{-8}$$
$$= 2.56 \times 10^{-7} - 7.3 \times 10^{-8}$$
$$= 1.83 \times 10^{-7}$$

for 
$$P = 75$$
 mm

$$T = 130^{\circ}F$$

In order to maintain the established tolerance that

$$\Delta n \leq 1.2 \times 10^{-7}$$

$$\Delta T \leq .65^{\circ} K$$

assuming adiabatic conditions at 1/10 atmosphere and 130°F temperature.

Experimental studies were carried out in an effort to confirm the critical effect of thermally induced index fluctuations. It was found that image quality was decidedly influenced by the pressure environment, and image quality improved with a decrease in pressure.

#### APPENDIX G

### DEVELOPMENT OF A LOW EMISSIVITY COATING SUITABLE FOR WINDOW APPLICATIONS

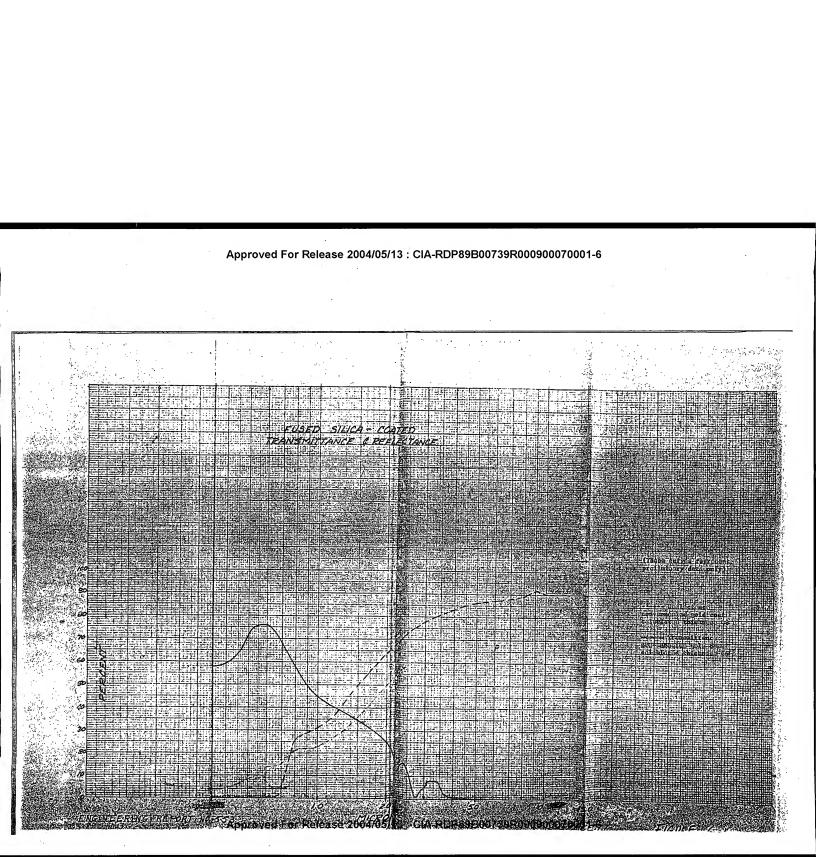
An investigation was carried out to ascertain what material could be used as a coating on the glazing surface which would provide high transmission properties in the region .4 to .7µ and high reflectance properties in the near and far infrared. Preliminary work indicated that a thin layer of gold might have the desired properties.

Several fused silica samples were coated with different thicknesses of gold, with a protective undercoat and overcoat. Spectrophotometer results indicate that transmittance, and electrical conductivity were dependent upon coating thickness for the thickness range of 5A to 60A investigated. Infinite resistance was exhibited by the thinner coatings. The coating which exhibited the most desirable optical properties had a resistance of 22 ohms/square, an integrated transmission of 70% in the visible region, and an integrated emissivity of 0.2. Figure G-1 shows the transmittance and reflectance values for a 47A coating on a fused silica substrate. Emissivity was calculated on the basis of:

$$(= 1 - (T_{meas} + R_{meas}))$$

The nature of the gold coating is such that it exhibits the tendency to change its properties under certain thermal conditions. Tests were carried out to determine whether the coating would breakdown in the temperature range for which it would be used. Tests so far have produced the following results:

1. Coatings on fused silica and glass, subjected to temperatures



up to 600°F for as long as 24 hours have maintained, to a first order, their original electrical properties.

2. Some samples, on glass substrates, subjected to 900°F environments, have changed properties within 1/2 hour of heating. The resistance has been infinite, indicating that the optical properties, in the infrared region, have become undesirable.

The emissivity of several coatings were measured at temperatures exceeding 600°F. Preliminary analysis of the data indicates that the emissivity at these temperatures is different than the emissivity at room temperature, and that the emissivity is effected by the thermal history of the sample.

Further testing is being carried out in an attempt to determine the basic nature of this breakdown. However, the results to data indicate that the coatings, on fused silica, are satisfactory for the temperature range up to 600°F; below the maximum they would be subjected to in the window configuration.

The electrical properties of the coatings make the coatings useful for several other desirable applications in the window configuration. They can be used as a means for resistive heating. In addition, the electrical continuity which they cause the window to have, provides the appearance of an electrical continuous skin when mounted in the vehicle.

For the case of a vacuum gap between two glazings, the low emissivity coating is used to limit heat transfer by radiation. The relative effectiveness of a coating on either side of the gap can be analyzed. Consider two surfaces, A<sub>1</sub> and A<sub>2</sub>, at temperatures T<sub>1</sub> and T<sub>2</sub>. The net heat radiation exchange between the two surfaces can be expressed as follows:

Let  $\epsilon_l$  and  $\epsilon_2$  = emissivity of surface A1 and A2 respectively.

 $W_1$  and  $W_2$  = total emissive power of  $A_1$  and  $A_2$  respectively  $r_1$  and  $r_2$  = reflectivity of  $A_1$  and  $A_2$  respectively.

 $F_2$  = fraction of energy leaving  $A_1$  and falling on  $A_2$ 

 $F_1$  = fraction of energy leaving  $A_2$  and falling on  $A_1$ 

The total energy that leaves surface  $A_1$  and falls on surface  $A_2$  is given by 1:

$$q_{1-2} = \frac{\epsilon_1 W_1 A_1 F_1 + \epsilon_2 W_2 A_2 r_1 F_1 F_2}{1 - r_1 r_2 F_1 F_2}$$

The total energy that leaves surface  $A_2$  and falls on surface  $A_1$ is given by:

$$q_{2-1} = \underbrace{\epsilon_2 w_2 A_2 F_1 + \epsilon_1 w_1 A_1 r_2 F_1 F_2}_{1 - r_1 r_2 F_1 F_2}$$

The net heat-radiation transfer between the two surfaces is, therefore

$$q = q_{1-2} - q_{2-1}$$

If  $W_1$  is replaced by  $\sigma T_1^4$  and  $W_2$  is replaced by  $\sigma T_2^4$ , then  $q = \underline{\underline{\underline{\sigma}A_1}} (\underline{\epsilon_1 T_1}^4 \underline{F_2} - \underline{\epsilon_2 T_2}^4 \underline{F_1 A_1} + \underline{r_1 \epsilon_2 T_2}^4 \underline{A_1 F_1 F_2} - \underline{r_2 \epsilon_1 T_1}^4 \underline{F_1 F_2})$   $1 - \underline{r_1 r_2 F_1 F_2}$ 

However for two parallel plates with equal areas,  $A_1 = A_2$  and Thus the above relation for the net-radiation heat transfer  $\mathbf{F_1} = \mathbf{F_2} = \mathbf{1}.$ reduces to

$$q = \frac{\sigma A_1 \xi_1 \xi_2}{\xi_1 + \xi_2 - \xi_1 \xi_2} (T_1^4 - T_2^4)$$

A.J. Brown & S.M. Maro, "Introduction to Heat Transfer", Third Edition, McGraw Hill Book Co., Inc., 1958

Therefore, we see that the effectiveness of a coating on oneparallel plate is the same regardless to which parallel plate the coating is applied.

The relative effectiveness of one coating in the first gap; one coating in the second gap; and two coatings, one in each gap was analyzed on the analog computer. Figure G-2 is an example of the results. It is clearly indicated that two coatings are desirable, and that if only one coating can be used it should be located in the outer gap.

ONE COATING, EACH GAP

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#### APPENDIX H

#### MECHANICAL CONSIDERATIONS TO WINDOW CONFIGURATION

Only preliminary investigations have been carried out for determining actual mechanical values, since considerations have been limited to general cases. It has been found that, from a mechanical standpoint, material choice is dictated by thermal shock considerations; and that glazing thickness is dictated primarily by size and pressure.

Mechanical properties of suitable materials is listed in Figure H-1.

#### THERMAL SHOCK

When a material is subjected to a temperature gradient, adjacent fibers tend to expand in differing amounts. Any constraint prevents the individual expansion of each fiber, thus setting up a system of thermal strains and associated stresses. When the thermal stress is generated by sudden changes in temperature, the action is referred to as thermal shock.

Since glass fails in tension, and usually at the surface, the temporary stresses from sudden cooling are much more severe than those resulting from sudden heating. The most severe thermal shock application in the window appears to be during intermittent cooling in the second gap.

The maximum temperature increment between the cooling air and the glazing surface is a function of the Modulus of Elasticity, the Coefficient of thermal expansion, Poisson's ratio and the allowable working stress of the material. Thus,

$$T = \underbrace{6t (1-\gamma)}_{I \in \mathcal{C}}$$

where  $\alpha$  = thermal expansion,  $\frac{1}{\log_{\mathbb{R}}}$ 

E = Young's Modulus, psi

 $\gamma$  = Poisson's Ratio

6. = Allowable Working stress, psi
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## FIGURE H-1

# COMPARISON OF MECHANICAL PROPERTIES \*

		1723 Aluminosilicate	7900 Vycor	7940 Fused Silica
YOUNG'S MODULUS P	si	12.8 × 10 6	9.6 * 10 6	10.5 × 106
Poisson's RATIO		0.22	0.181	0.17
HARDNESS (KNOOP)		595 100	630 <sup>50</sup>	644 <sup>so</sup>
Mod. of Rupture ** P	sí	9.3 × 10 <sup>3</sup>	7.13 × 10 <sup>3</sup>	8.0 × 10 <sup>3</sup>
DENSITY LL	H3	164.0	136.1	137.3
Expansion 10-7/	°F	25.3	4.4	3.0

<sup>\*</sup> Data from Corning Glass Works (AF 33(600)36852) Quarterly Report No.1
\*\* Abraded Annealed.

For a maximum allowable tensile stress of 1000 psi, Corning 7940 fused silica can withstand a  $\triangle T$  of  $263^{\circ}F$ . Under the same conditions, Soda Lime (BK-7) can only withstand a  $\triangle T$  of  $17^{\circ}F$ . Based on this analysis, BK-7 should not be used as the inside glazing. Table H-2 lists the thermal shock resistance for several glazing materials.

TABLE H-2

#### THERMAL SHOCK RESISTANCE

Glazing Material	<b>∆ T</b> *
7940 Fused Silica	263 <sup>0</sup> F
7900 Vycor	194 <sup>0</sup> F
1723 Aluminosilicate	24°F
0080 Soda Lime	17°F

<sup>\*</sup> where AT = (T<sub>surface</sub> -T<sub>air</sub>)

No experiments have been performed to verify the figures in Table H-2. The main factor which would influence these tabulated values is the allowable working stress of 1000 psi. Breaking stress is very dependent upon conditions of the glass, annealing, and surface quality. Allowable  $\Delta T$  varies directly with increasing working stress.

The analysis upon which the determination of allowable  $\Delta T$  is based is independent of glazing thickness. Experimental results listed by Corning\* indicate a thickness dependence of  $\Delta T$ , where the  $\Delta T$  tolerance increases for decreasing thickness. Values calculated in Table H-2 are within expected agreement with the Corning data.

In addition, it should be pointed out that  $\Delta$  T represents the short term cooling temperature drop of the glazing surface. The factor of a film heat transfer coefficient means that the cooling air introduced may have a temperature difference with respect to the glazing surface greater than  $\Delta$  T. The magnitude of this coefficient has not yet been investigated.

<sup>\*</sup> Properties of Selected Commercial Glasses; Corning Glass Works; Corning, N.Y. Approved For Release 2004/05/13: CIA-RDP89B00739R000900070001-6

#### THICKNESS

The thickness of the glazings were calculated based on the pressure distribution shown in Figure H-3. The glazings were assumed to be simply supported on a rigid frame. Stresses and deflections would be slightly smaller for glazings with fixed edges on a rigid frame.

		Time 1	Time 2
	inside	3_psi	3_psi_
	С		
		5-0 psi	5-0 psi
\	В		
		0 psi	0 psi
)	A		
	outside	0 psi	3.5 psi

#### Figure H-3

Taking 1000 psi as the maximum allowable tensile stress, the minimum thicknesses of glazings A, B & C are about .6", .75" and .6" respectively.

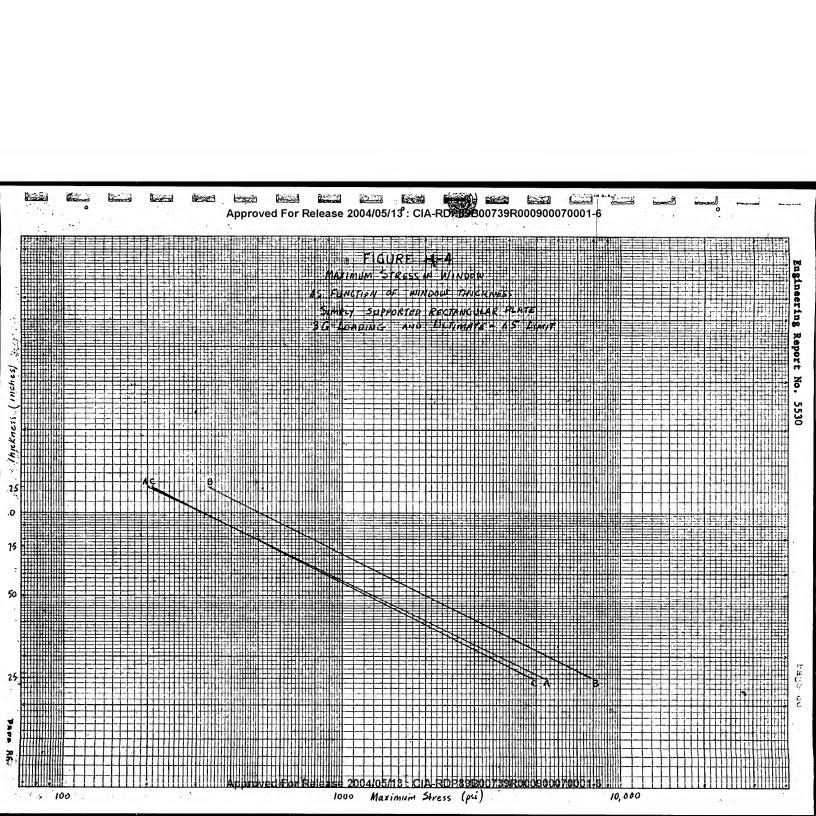
Curves of stress vs. thickness, and deflection vs. thickness are presented in Figures H-4 and H-5.

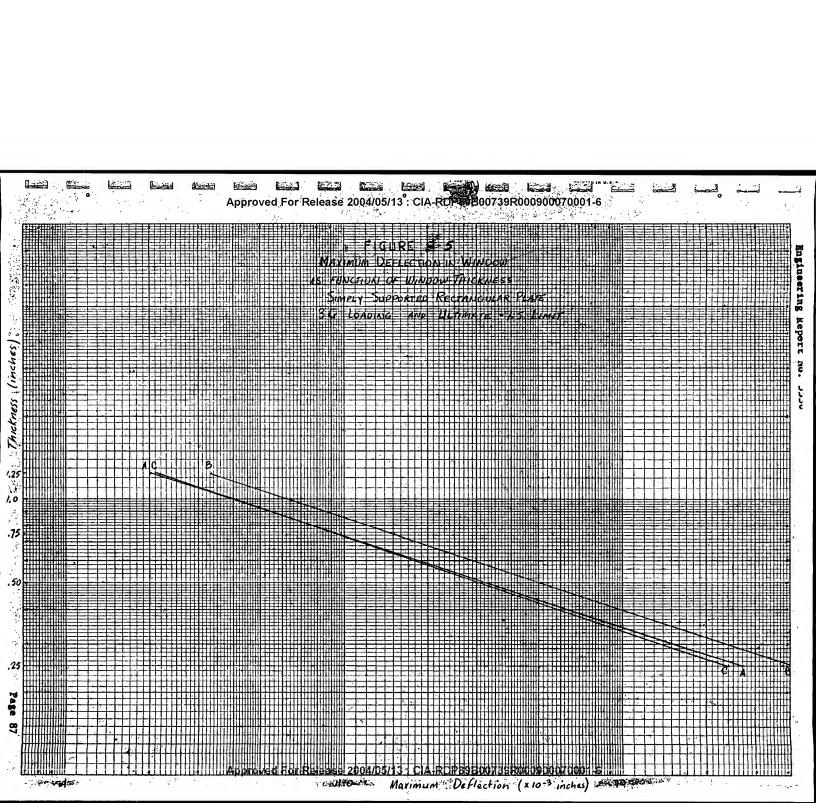
Figure: H-6 is a plot of the stresses in glazing A with a pressure differential of 15 psia across the glazing. A pressure differential of this magnitude requires a thickness of 1.25" for glazing A.

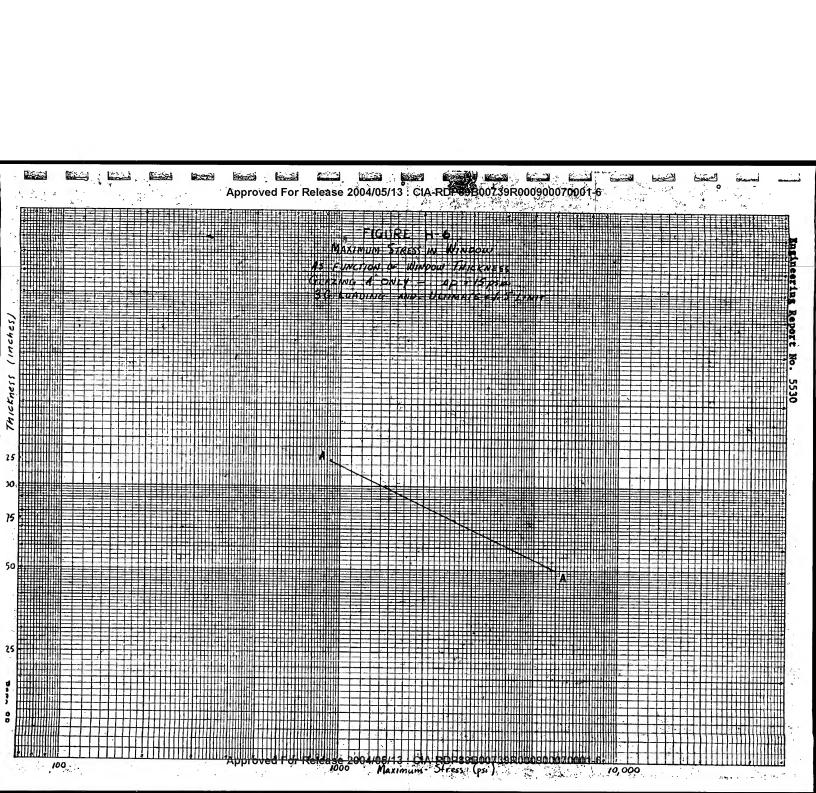
The pressure profiles demonstrated in Figure H-3 are realistic of actual pressures if the necessary vacuum between glazings A and B is established after altitude is reached, and bled prior to landing. The condition of 15 psia differential represented in Figure H-6 would be for establishing a hermetically sealed vacuum on the ground.

For the specific case of the 24-inch Schmidt system, the approximate window size necessary is 10.5 x 18.5 inches. The following is the analysis for determining glazing thickness for this case.

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**ANALYSIS** 

The maximum tensile stress in a simply supported plate is

$$\sigma_{\text{max}} = \frac{6 \, \theta \, q \, a^2}{h^2}$$

where  $\xi$  = .0994, a dimensionless quantity depending on  $\frac{b}{a}$  and  $\sqrt{\phantom{a}}$ 

h = thickness of plate, i.

q = uniform loadings, psi

a = smaller dimension, in.

q = Ph psi

... 
$$G_{\text{max}} = \frac{0.596 \left[G \in h \neq P\right] (10.5)^2 F}{h^2}$$

where G = "G" loading

P - pressure differential across plate

F = design factor

The maximum deflection in a simply supported plate is

$$\delta \max = \frac{\alpha q a^4}{E h^3}$$

where  $\alpha = 0.1060$ , a dimensionless quantity depending on  $\frac{b}{a}$  and

q = uniform loading, psi

h = thickness,

a = smaller dimension,

E = Young's Modulus, psi

$$\frac{10.5 \times 10^{6} \text{ max}}{10.5 \times 10^{6} \text{ h}^{3}}$$

where G = "G" loading

P = pressure differential across plate.

#### APPENDIX I

#### TECHNICAL SUMMARY - WINDOW CONFIGURATION

The most suitable environment, in order to maintain the desired image quality, minimizes or eliminates index fluctuations in the optical path. This dictates an isothermal equipment bay concept. The equipment, bay walls, and—inner-window surface should-be-kept-at the same temperature. If this is accomplished, it will eliminate heat transfer either into the equipment bay, or from one part of the bay to the other; and this will eliminate index fluctations from thermal gradients and resulting pressure changes.

The tolerance on acceptable temperature fluctuations within the equipment bay increases with decreasing equipment bay pressure. Realistically achievable temperature controls are possible at atmospheres no greater than about 75 mm Hg.

It is desirable to maintain minimum temperature drop through the glazing materials themselves, in order to reduce optical wavefront deformation due to index changes. In addition, this will enable thinner glazings to be used, making a more suitable mechanical configuration. The most desirable location for the maximum temperature drop is across the gaps between the window glazings. Since air has a much lower thermal conductivity than the glazing materials, a maximum temperature difference across the gaps is a natural consequence. In order to do this, however, it is necessary to limit or eliminate heat flow from hot to cooler glazings. In order to eliminate heat conduction and convection, vacuum of the order of 5 x 10<sup>-3</sup> mm Hg must be maintained (because the thermal conductivity of air is independent of density until the pressures become so low that the mean free path of the air molecules is comparable to the dimension of the gap). In order to limit radiation, a low emissivity coating should be applied to one surface bordering the gap.

It is of no consequence to which side of the gap the coating is applied. A

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low emissivity coating is most effective in the outermost gap, and two coatings are more effective than one. If only one coating is used, it should be located in the outer gap.

In addition to its low emissivity properties the coating will serve as a conductor across the window, therefore, maintaining the appearance of an electrically continuous skin.

In order to maintain the inner surface of the window glazing at a constant and tolerable temperature, cooling or heat removal from the window glazings must be present. The use of cool air for heat removal is recommended. For the same considerations which dictate the desirability of eliminating air in the equipment buy, it is desirable to eliminate the cooling air from the gaps during a photographic exposure. This can be accomplished by using cooling air only during that portion of the photographic cycle during which no photograph is being taken. For the 24" SchmidteScanning System, this appears feasible. A cycle of about 3.6 seconds on and 3.6 seconds off is recommended. The use of cyclic cooling requires that cooling air can be introduced, then removed, and a low density atmosphere be reestablished within the allowable cooling cycle time. This seems quite feasible if about 0.3 cubic feet/min. of cooling air can be dumped overboard. Cooling air temperature and rate must still be finalized.

During two portions of the mission profile there is a heat drain to the outside, resulting in a cooling of the inner glazing. Depending on allowable temperature fluctuations of the inner surface, heating may be required in the inner gap. This can be accomplished either by introducing hot air or by resistive heating of the conductive gold coat, if a gold coat is present.

As a maximum tolerance, the net deviation from a linear thermal gradient across the pupil cannot exceed 0.6 F per inch. It would be desirable

to use aluminosilicate for outer glazing due to the fact that its expansion properties are more nearly similar to those of the vehicle skin than are the expansion properties of fused silica. However, thermal shock and optical considerations indicate that the use of fused silica would be desirable. Further investigation is recommended to finalize material choice. At least the two inner glazings, subject to large thermal shocks from the cycled cooling air, should be fused silica.

The approximate window size for the 24-inch Schmidt-System is 10.5 x 18.5 inches with slightly rounded corners and edges. The thickness of the glazings have been calculated on the basis of establishing a vacuum in the first gap after altitude has been attained, and bleeding prior to landing, in order to avoid a 15 psi differential. Calculated thicknesses are 0.6, 0.75, and 0.6 inches from outer to inner glazings.

The dynamic deflection of the window glazings for these thicknesses is not sufficient to exceed the tolerances established to maintain desired image quality.

These considerations dictate a basic window configuration concept. The three glazing configurations shown in Figure I-1 embodies all these concepts. One side of each gap is coated with a gold coating of 0.2 emissivity. Regulated cooling air is cycled through the inner gap, to maintain the inner window surface at  $130^{\circ}$ F. The bay environment, at a pressure of 0.3 pounds per square inch, is maintained to provide temperature fluctuations no greater than  $\frac{1}{1}$ °F.

#### APPENDIX J

#### FILM TRANSPORT

This area may be divided into two significant aspects. The first will consist of the arrangement to transport the film at an accurately programmed velocity; and, the second will consist of arrangements to persuade the film to conform to a selected geometric-velocity configuration during its travel past the slit.

Investigations of the accuracies in the velocity of film travel suggest that a servo control is indicated. Analysis of this problem will continue.

In the second aspect of the film transport there are unique and critical design parameters which must be satisfied. Calculations and empirical investigations have been made in some of these areas. Thin base film requires special handling because it will damage easily. The film transport arrangement must facilitate positive film registration without the advantage of sprocket holes and it must also allow for unavoidable slack caused by momentary power or component failures, film splices and other imperfections in the film. In a temative optical design, the ideal focal surface would be a 30-inch radius sphere. However, a sphere of this size is not practical and some compromise in the shape of the focal surface is indicated. A ten-inch long roller with a 30-inch radius profile in the axial plane and a maximum radial length of 15/16 inches was fabricated. This roller (platen roller) is the pressure plate in the film transport breadboard system constructed to test the behavior of thin base film. The breadboard will prove a valuable tool as it can be readily modified for testing of other transport systems. (See Figure J-1).

When the unit was put into operation the following facts were noted:

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- A. The film did not easily stretch over the platen roller.

  Calculations indicate that approximately 150 pounds tension would be required to achieve the amount of stretch desired.

  However, from the breadboard it was found that severe stretching produced buckle areas. Pressure and localized heat resulting from the crimping of the film might expose the film.
- B. In an effort to stretch the film completely over the barrelshaped platen roller, concave profiled rollers were substituted
  for the straight cylindrical rollers which are located adjacent
  to the platen roller. This arrangement permitted more film to
  stretch over the barrel with no increase in tension. It was
  not possible, in any of the tests conducted so far, to obtain
  intimate contact between the barrel and the entire 9 1/2 inches
  width of the film.

The most exact method to simulate a spherical focal surface would be to have a fixed, highly polished spherical section and allow the film to file over it. The detrimental effects of sliding, if any are appreciable, will be established by tests.

Another approach would be to have a plastic belt contoured to the desired shape and permit the film to travel with this belt. The slip between the film and the platen roller present in the other systems would, in such a system, occur between the plastic belt and the guiding roller.

Analysis of the velocities of film transported over contoured rollers shows that the center of the film will travel 3.2% faster than the edges. For the same width film on a 30-inch radius sphere, the percentage variation between the center of the film and the edges would be 1.2%. A compromise condition may be indicated.

The platen roller is barrel-shaped and as such it has different tangential velocities along its axial length. These velocities vary as much Approved For Release 2004/05/13: CIA-RDP89B00739R000900070001-6

as 60%. Since all elements on the film travel almost at the same velocity and since the surface of the roller rotates at different velocities, there is slip between the film and the roller. Total slip over the platen area may be expressed as follows:

Distance across slit = .25"1

Velocity of film = 10"/sec

Time to pass slit = 25/10 = .025 sec

With 60% slip ( V = 10"/sec - 4"/sec) = 6"/sec D = 6"/sec x.025 sec = .150"

.15 represents 60% of surface and a deformation of film caused by abrasion or friction of heat would be intolerable.

Assuming a two-pound normal force between the film and the platen, the heat generated will be approximately .92 watts. Investigation of ambient conditions and length of operation should indicate if heat can be removed from the critical roller surface should be this be necessary.

A method of reducing the relative slip is under investigation

and indications are that if a composite roller is fabricated, the slip can

be held to a selected figure. The composite roller would consist of a number

of individual rollers mounted on the same axis and whose integrated surface

profile would duplicate that of the original single roller.

Finally, the tolerance of .0005 inches required in the focal depth is possible in the static configuration. Dynamic conditions may dictate unconventional approaches.

#### APPENDIX K

#### SKID TURN FILM ROLLER

The system may require that the film path incorporate a compound bend. This is accomplished by passing the film over the roller at an angle other than 90° with the axis of rotation of the roller. This angle relation produces a velocity vector parallel to the axis of rotation. If the roller does not move in the same direction as the resultant vector, slip will occur. This slip is eliminated by moving, parallel to the axis of rotation, that portion of the roller which is in contact with the film an amount equal to the axial vector transmitted by the film to the roller. Therefore this directional roller will consist of a number of axial elements which experience identical angular motion but are independent from each other in their axial confines. Calculations to determine exial length of roller reveal that for a 9-1/2 inch wide film the minimum length required for static accommodation of film is 14.433 inches. The additional length required by the dynamic conditions is a function of angle of wrap, lead angle and number of sliding elements. This figure is 1.309 inches. The total length of roller is 14.433 + 1.309 = 15.742 inches. The axial movement of the elements will be accomplished by cams. This arrangement relieves the film from the burden of moving the sliding elements through friction.

A second method of achieving a compound bend is to have the film pass over a cushion of air emanating from a stationary bar element. Such a device has been used successfully in existing systems.

#### APPENDIX L

#### CEMENTED JOINTS

When light-weight structures are considered, normally honeycomblike structures are conceptually attractive. If these are fabricated by
methods which dimple the skin member, such as welding, strength can be
substantially reduced. Similarly, fabrication by mechanical joining, as with
bolts or rivets, may have the same effect. Consequently, it becomes attractive
to consider chemical joining by methods, such as bonding, in which the
mechanical shape of the structure is not altered.

Another reason for considering cemented joints results from the difficulty of machining magnesium and beryllium. These two metals have very high strength and rigidity to weight ratios and they also have very high internal damping. As a consequence of this desirable combination of properties, it is attractive to utilize these materials if it can be done practically; and this is partially dependent on the ability to fabricate cemented boints.

#### APPENDIX M

#### OPTICAL POWER SPECTRUM ANALYZER

The power spectrum analyser is a device intended to indicate the amplitude and direction of the frequency components of the image structure of a transparency. If the transparency is a negative or positive photograph, the analyser will immediately give the resolving power of the photographic system used (the maximum frequency obtained by the analyzer), and the relative content and distribution of the frequency components passed by the photographic system. Different types of scenes will have different distributions, although any given distribution will have a whole class of scenes corresponding to it.

#### THEORY OF OPERATION:

The operation of the power spectrum analyzer is based on the fact that the Fraunhofer image of a point source produced by a diffracting screen is the Fourier transform of the wave amplitude in the plane of the screen. If f(x,y) represents the wave amplitude in the plane of the diffracting screen and  $\psi(E_x, k_y)$  represents the amplitude of the image where  $(k_x, k_y)$  is the normalized coordinate of a point in the image plane, then

$$\psi(k_x, k_y) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) e^{i(k_x \times + k_y y)} dxdy Eq. (1)$$

In practice f(x, y) is limited to the pupil of an optical system and is zero outside the pupil, and the integral can be restricted to the area of the pupil. It can be seen that  $k_x$  and  $k_y$  which are position coordinates in the image plane correspond to frequency components in the plane of the diffracting screen.

The value of the normalized coordinate is given by

$$k = \frac{2\pi}{\lambda} \sin \theta \qquad \qquad \text{Eq. (2)}$$

where  $\lambda$  is the wavelength of the light and  $\theta$  is the angle of diffraction. The actual position (x', y') in the image plane as a function of the actual spatial frequency component  $(\mathcal{V}_x, \mathcal{V}_y)$  in the plane of the diffracting screen is given by

$$X'=f \tan \theta_X$$
,  $y'=f \tan \theta_y$ , and Eq. (3a)   
  $\sin \theta = \lambda \nu$ .

The wave amplitude f(x, y) may be complex; that is, it may represent both variations in the magnitude and phase of the wave across the pupil containing the diffracting screen. This phase variation can have a strong effect on the image and is unwanted in the power spectrum analyzer. The manner of its control and the degree to which it can be tolerated will be discussed later. For the present we shall assume that the phase variation is negligible.

Although the phase variation may be negligible in the pupil, phase variations will exist in the image plane depending on the particular geometry of the diffracting screen.

It should be emphasized that the function we are analyzing is the amplitude of the wave in the pupil as modified by the diffracting screen. The transmission of a screen is usually in terms of the intensity of the light transmitted which is the square of the amplitude transmitted if there is no phase variation.

The diffracted image observed is also the intensity of the wave in the image plane rather than the amplitude, and is the product of the amplitude and its complex conjugate.

The amplitude in the image plane is the Fourier transform of the amplitude in the pupil plane. Thus the intensity of the image is the product of this Fourier transform and its complex conjugate. This product is commonly known as

the power spectrum (thus the name of the instrument) and is the Fourier transform of the autocorrelation function of the diffracting screen.

Since the power spectrum has eliminated the phase information (the product of a function and its complex conjugate is the square of the modulus of the function), any given power spectrum corresponds to a whole class of objects which differ from each other only in the manner in which the structural details are distributed, and thus is a statistical measure of the structural content of the object.

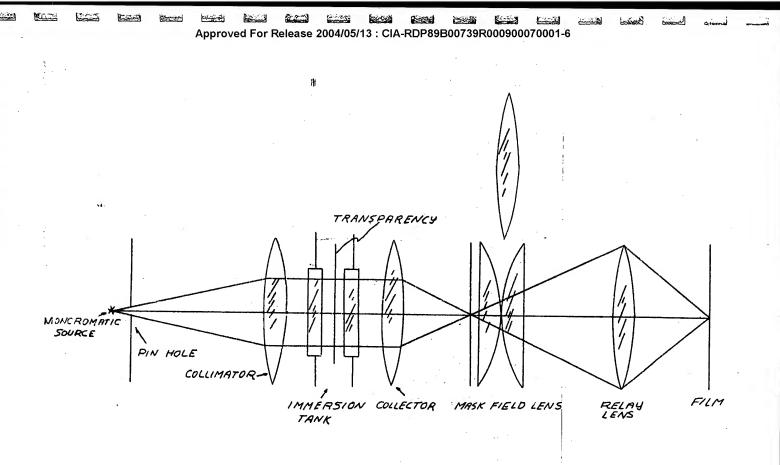
The power spectrum analyzer is intended to measure the structural content of the image of a transparency (as measured by its amplitude transmission) by presenting its power spectrum graphically as the variation in intensity of a point image resulting from diffraction by the transparency. The intensity at any point in the image plane is directly proportional to the power spectrum density of that frequency component of the transparency having a frequency proportional to the distance of the point from the center of the image and a direction determined by the direction of the point from the center of the image.

### DESCRIPTION OF INSTRUMENT:

Sec.

A monochromatic light source, pinhole, and collimator serve to provide monochromatic plane waves incident on the transparency. An immersion tank is provided to reduce phase variations in transmission to a minimum. A collector lens forms an image of the pinhole after the light has been diffracted by the transparency.

This image is the power spectrum desired, and a sheet of film inserted here would record the image. However, in most cases the center of the image, corresponding to zero frequency, contains an appreciable fraction, frequently more



than half, of the total energy, and the rest is distributed over a large area.

If the exposure is sufficient to record the major part of the power spectrum,

the center will be heavily overexposed and much of the power spectrum will be

spread over by irradiation from the center image.

To reduce this effect to a minimum a mask consisting of an opaque central spot is inserted in this image plane and the image is relayed to a more convenient location by a relay lens.

The calibration of the frequency scale is most easily done by inserting a grating of known frequency, such as a Ronchi grating, in the immersion tank and recording its image. The fundamental and its harmonics will be recorded, providing an accurate frequency reference.

A check on the reliability of the system can be made by taking a picture of the image when the transparency is removed. If the mask is also removed, the point image obtained will represent the weighting function of the power spectrum measurement. The intensity at any point in the image plane is not strictly proportional to the power spectrum density of the corresponding frequency, but to a weighted average for that frequency and its neighboring frequencies. The spread of the point image with the transparency removed will represent the weighting function.

The main effect of enlargement of this image will be a corresponding change in the weighting function. This includes slow variations in phase, such as occurs in the presence of aberrations. Such slow variations will have no high frequency components. However, another effect of the slow phase variations is a weighting of the areas of the transparency in their contributions to the power spectrum. If the transparency does not have homogeneous texture, different aberration distributions will result in slightly different power spectra.

If the power spectrum itself is not expected to have fine structure, a relatively large weighting function is telerable. The most efficient use of this

tolerance is the enlargement of the pinhole. The pinhole image is compact so that the weighting does not extend too far out, but the increase in transmitted energy, and consequent reduction in exposure time is considerable.

A picture taken with the transparency removed but the mask in place will show how much light will be spread by the strong zero-frequency component in spite of the central mask. This residual light is a result of the unlimited, although low-level, diffraction spread; scattered light, and out-of-focus ghost images. The diffraction spread is generally very small, the scattered light can be kept at a minimum by having a clean and well-baffled optical system, and the ghost images can be kept to a minimum by means of low-reflection coatings. EXPERIMENTAL RESULTS:

Figures M-1, M-2, M-3 and M-4 show some power spectra obtained with this instrument along with contact prints of the corresponding transparencies which were used as diffracting screens, and enlargements of selected portions of the transparencies.

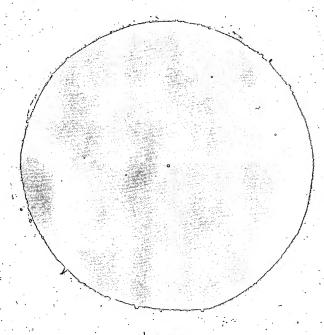
The power spectrum of the Ronchi grating shows the fundamental and harmonics of the structure. If the lines and spaces were exactly equal in width, the even harmonics would be absent. Their presence, although they are noticeably weak, indicates that the lines and spaces are not exactly equal. This grating was used to calibrate the frequency scale.

Two of the remaining pictures were taken with a relatively low-resolution system and the third with a high-resolution system. The low-resolution system was limited to about 13 lines per mm. The high resolution system was limited to about 30 lines per mm.

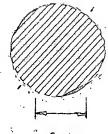
One of the low-resolution pictures is of a river bed with foliage and the other is of a developed area. The river-bed picture has a power spectrum consisting of a broad, generally undifferentiated spread with a diffuse bar across Approved For Release 2004/05/13 : CIA-RDP89B00739R000900070001-6



FOWER SPECTRA OF SCENE



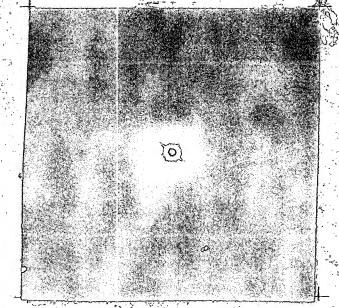
SCENE RONCEI GRATING - 5.2 lines/mm.



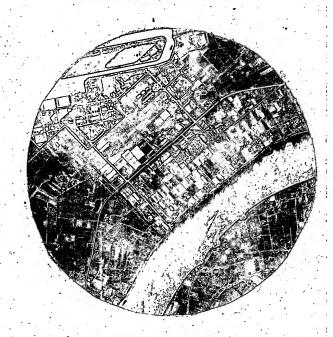
1. Then

SCHNE ENLARGEMENT





POWER SPECTRA OF SCHOOL



HIGH RESOLUTION SCENE FORULATED AREA

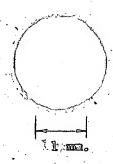
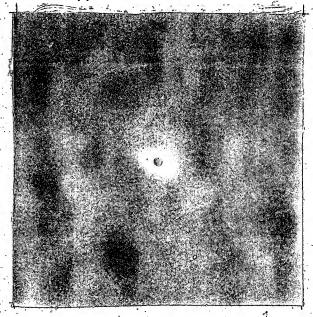


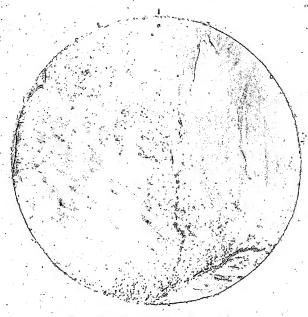
Figure M-2

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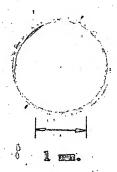
# Approved For Release 2004/05/13 : CIA-RDP89B00739R000900070001-6

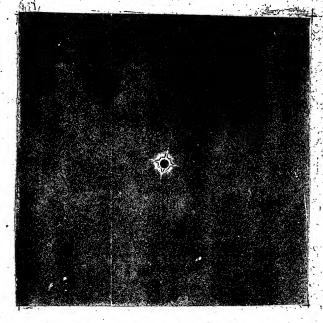


POWER SPECTRA OF SCHNE

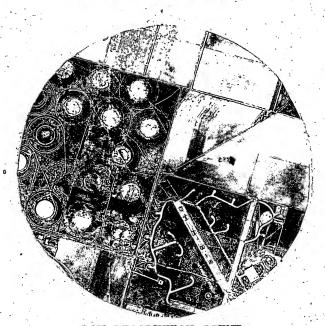


Lou resolution ecene river valley

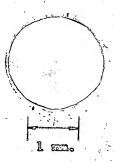




POWER SPECTRA OF SCHIE



LOW RESOLUTION SCENE FORULATED AREA



it in one direction. The broad spread indicates a generally random structure.

The bar correlates with the direction of illumination of the scene, the shadow being very roughly linear and oriented in the same direction.

The power spectrum of the developed area shows strong spikes oriented along the principal directions of the artifical structure with almost no power associated with the frequencies oriented otherwise. One of these principal spikes shows nodes indicating regular periodic structure covering an appreciable area of the transparency. On examination it can be seen that plowed fields correspond to the nodes.

The high-resolution picture is also of a developed area, and this is again reflected in the strongly spiked structure of the power spectrum. This picture also has a plowed field, but the relative area is small and the nodes are not apparent.

#### APPENDIX N

#### IMAGE MOTION COMPENSATION

The present IMC problem is concerned with a slit camera which scans laterally, while the vehicle carrying it moves forward (see Figure N-1). The scan axis is parallel to the line of flight and the optical axis intersects the nadir when the scan angle is zero. In the figure, h is the altitude,  $\underline{\mathbf{v}}$  the forward velocity,  $\underline{\mathbf{p}}$  the scan angle,  $\underline{\mathbf{x}}$  the field angle and  $\underline{\mathbf{f}}$  the focal length.

The objective of an IMC technique is to move the film and/or the image in such a way that the relative velocity between the two is negligibly small. The most direct way of approaching the problem is to refer the coordinate system to the surface defined by the slit and to develop the equations of motion of the image relative to the slit as a function of  $\underline{v}$ ,  $\underline{h}$ ,  $\underline{f}$ ,  $\underline{\hookrightarrow}$ , and  $\underline{B}$ . Two types of focal surface will be considered—the sphere and the plane.

### INSTANTANEOUS IMAGE VELOCITIES

Figure N-2 illustrates the derivation of the image velocity in the plane of the slit. Table N-3 shows the image velocity relationships.

An interesting fact is that the image velocity in the plane focal surface is independent of the field angle x whereas the spherical focal surface is not.

### IMC TECHNIQUES

The simplest scan rate is a constant rate. In order to achieve a required overlap  $\underline{p}$  with a given maximum field angle  $\underline{\alpha}_{\underline{m}}$ , the scan rate is given by

$$\frac{d\mathbf{g}}{dt} = \frac{\mathbf{W}_4 \cdot \mathbf{v} \cdot \cot \alpha_{\mathbf{m}}}{(1-\mathbf{p})} \tag{1}$$

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F | G N-| Approved For Release 2004/05/13 : CIA-RDP89B00739R000900070001-6

FIG N-2
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# TABLE N-3 IMAGE VELOCITY RELATIONSHIPS

المستنفق

# SPHERICAL FOCAL SURFACE

$$\frac{d\alpha}{dt} = \frac{V}{h} \cos^2 \alpha \cos \beta$$

$$V_y = f \frac{d\alpha}{d+} = f \cdot \frac{V}{h} \cdot \cos^2 \alpha \cos \beta$$

$$\tan \phi = \frac{\frac{1}{h}\cos \alpha \cos \beta}{\frac{d\beta}{dt}}$$

$$V_{r} = V_{x} \quad sec d = f \cdot cos. \propto sec. \phi \cdot \frac{d\beta}{d+}$$

$$= V_{y} \quad csc. \phi = f \cdot \frac{V}{h} \cdot cos.^{2} \propto cos. \beta \quad csc. \phi$$

# PLANE FOCAL SURFACE

$$\frac{d\alpha}{d+} = \frac{V}{h} \cos^2 \alpha \cos \beta$$

$$V_y = f SEC^2 \propto \frac{d\alpha}{dt} = f \cdot \frac{v}{h} \cdot \cos \beta$$

$$V_x = f \frac{d\beta}{d+}$$

$$V_r = V_x$$
 sec  $d = f \cdot sec \phi \cdot \frac{d\beta}{d+}$   
=  $V_y$  csc.  $\phi = f \cdot \frac{Y}{h} \cdot cos \beta$  csc  $\phi$ 

in radians per second, assuming that successive scans are  $90^{\circ}$  ( $\pi/2$  radians) apart.

The components of image velocity when scan rate is constant are as follows: the lateral velocity component  $v_x$  is constant; the longitudinal component  $v_y$  varies directly as  $\cos \beta$ ; and  $\beta = \frac{d\beta}{dt}$  t. Thus, neglecting the field angle factor for the spherical focal surface, perfect compensation may be achieved by using a constant scan rate, a constant film velocity in the lateral direction and film motion varying as  $\cos \beta$  in the longitudinal direction.

It may be that moving the film accurately in the longitudinal direction may be more difficult to achieve than accurately varying the scan rate and film velocity. In this case it would be preferable to keep  $\spadesuit$  constant by varying  $\frac{dB}{dt}$  so that it is proportional to  $\cos \beta$ . The film velocity will then be directly proportional to  $\frac{d\beta}{dt}$  and unchanging in its direction  $\spadesuit$ , which is no longer perpendicular to the scan axis. Then the differential equation

$$\frac{d\mathbf{g}}{dt} = A \cos \mathbf{\beta} \tag{2}$$

must be satisfied, where  $\underline{A} = \frac{v}{h} \cos \alpha \cot \phi$  for the spherical fical surface and  $\frac{v}{h} \cot \phi$  for the plane focal surface. The solution is

$$\tan (\beta/2 + \pi) = e^{At}. \tag{3}$$

 $\beta$  and  $\frac{d\beta}{dt}$  as a function of time are shown in Figure N-4.

Clearly, this mode of IMC is efficient only if relatively small scan angles are involved, whereas the previous method is unrestricted.

Four pictures are to be taken in one complete cycle but only 60° are used for each picture. Figure N-5 shows as a solid line those portions of the scan which must be matched accurately, the plot being one of scan rate versus time.

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Figure N-6 shows the result of trying to match the required variation by a simple sinusoidal variation of the rate given by

$$\frac{1}{A} \frac{dB}{dt} \bigg|^{*} = 1 - a(1 - \cos \psi) \tag{4}$$

where

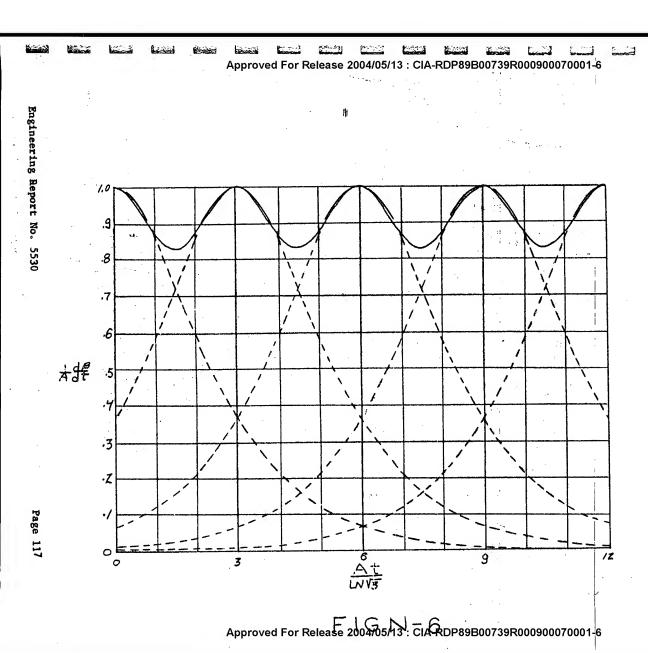
$$\gamma V = \frac{2\pi A}{3 \ln \sqrt{3}} t \tag{5}$$

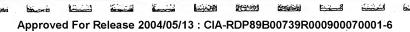
and a\_is\_determined\_to\_minimize the error.

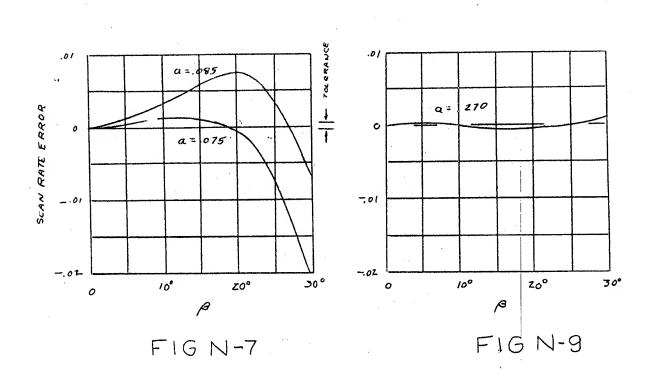
Figure N-7 shows the error as a function of the scan angle B for two values of a. The upper curve equalizes the positive and negative errors whereas the lower curve attempts to get the maximum scan range with the least error. It is apparent that this approximation would be adequate only over a range of about 15°.

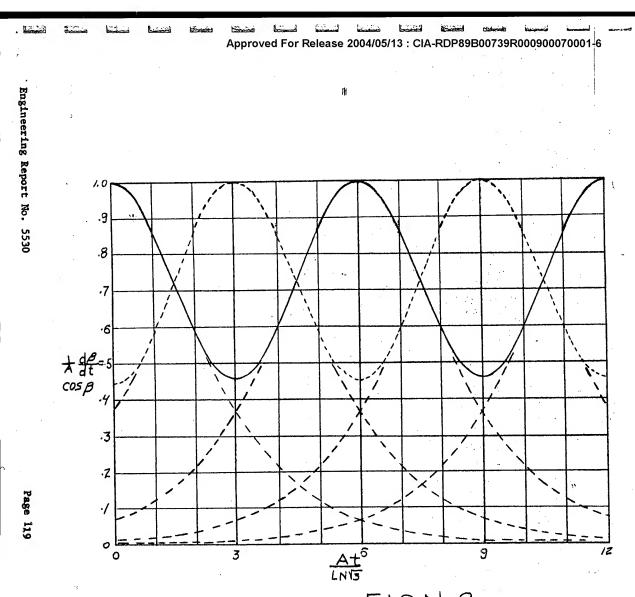
A possibility for achieving a good approximation to the scan rate variation for the scanning prisms is that each of the prisms is used only in every other scan. This is done by varying each of the prisms at only half the frequency given above and  $180^{\circ}$  out of phase with each other. This situation is desirable mechanically because of the automatic balancing of moments. Figure N-8 illustrates this method and Figure N-9 shows the error resulting. This approximation is adequate over the full  $30^{\circ}$  range.

However, the magnitude of the variation has gone from about 9% to 37% of the average rate. In addition, the film velocity variation must be obtained from a separate mechanism which will operate roughly as in Figure 5, but with a better fit.









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### APPENDIX O

## FILM EVALUATION EQUIPMENT

Several pieces of equipment, specifically designed for film evaluation, have been constructed. An arrangement consisting of a light source and two cameras is used for the production of targets and for the photography of those targets onto the film being evaluated. One camera-photographs-ronchi-rulings onto Kodak High Resolution Plates to produce targets having a frequency range of 4 to 15 lines per millimeter.

The second camera photographs targets at a 20% reduction onto the films being studied, offering a frequency range of 80 to 300 lines per mm. The camera employs a microscope apochromatic objective mounted in a precision focussing mount; a beam splitting plane and external light source in the optical path give the capability of introducing controlled non-image forming light which in effect reduces the contrast of the target image.

A plate processing rack and a film agitator were built for the precision processing of plates and films. The design emphasis was on even development over the emulsion surface and processing repeatability.

A Leeds and Northrup microphotometer is in the process of being modified. A ribbon filament lamp and an adjustable mechanical slit comprise the light source, and a photomultiplier as the output source activates a recorder. The size of the scanning slit is limited only by the sensitivity of the photomultiplier and associated amplifier.

## APPENDIX P

### PERTINENT DOCUMENTS LIST

The following is a list of pertinent documents concerning this

• •			•	<b>'</b>
_	program:			
	DATE	DOC. NO.	er Number	TITLE
<b>7.</b> 1.	1 February 1959	-	<b></b>	Aerial Reconnaissance System Progress Report No. 1
2.	2 March 1959	. 1	5394	High Acuity Reconnaissance Systems for A High Perform- ance Aircraft
3.	30 March 1959	5	an 40, 40 ar	Letter from JGB to Mr. B.
4.	13 April 1959	4	5414	Project Plan 13 April - 30 June 1959
5.	1 May 1959	15	5424	Progress Report No. 1 14 - 30 April 1959
6.	7 May 1959	17	• • • • • • • • • • • • • • • • • • •	Letter from MDR to LEW Evaluation plans
7.	28 May 1959	22	5442	Progress Report No. 2 1 - 28 May 1959
8.	28 May 1959	23	5443	Preliminary Considerations of Special Equipment for an Alter- nate Carrier
9.	22 June 1959	27		Letter from MDR to DRK Window
10.	26 June 1959	32	5465	Progress Report No. 3 29 May 1959 - 26 June 1959
]11.	2 July 1959	37		Quality Evaluation
12.	10 July 1959	39		Letter from MDR to LEW 5A & 5B n.g.
13.	20 July	<b>***</b>		Letter from RMS to LEW Catad. Systs.
14.	27 July 1959	40	5485	Progress Report No. 4 27 June 1959 - 24 July 1959
15.	31 July 1959	43 ;	/ /	Revised Side Views for Append. C - ER 5485
16.	24 August 1959	50	***	Information from August 19-20 Meeting re Payload Cooling
17.	1 September 1959	53		Letter from MDR to RSQ Trip Reports

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	DATE	DOC. NO.	er Number	TITLE
18.	4 September 1959	54		Letter from MDR to RSQ Sketches 5C and 6A
19.	10 September 1959	.57	5506	Progress Report No. 5 25 July - 9 September 1959
20.	15 September 1959	59	40 40 40 H	Configurations E, F, G, H
21.	12 October 1959	62	****	Selection of System
]22.	13 October 1959	63		Drawings 546-0900 thru 546-0903
]23.	20 October 1959	68		Project Plan and Budget Cost Estimate for Project
24.	20 October 1959	69	<b></b>	Potential Systems



